## COMP3506: Quiz 1

Name:

Student ID:

This is the quiz paper for COMP3506. If you are registered for COMP7505, turn overleaf.

Each of the following problems bears 10 marks.

**Problem 1.** Which of the following is *not* an atomic operation of the RAM model?

Answer: [

A. Calculate a + b where a and b are stored in two registers.

B. Sort an array of n integers for an arbitrary value of n.

**Problem 2.** Which of the following is true? Answer:

A.  $n \log_2 n = O(n)$ . B.  $n = O(n \log n)$ .

**Problem 3.** Which of the following is true? Answer:

A.  $n^2 = \Omega(n)$ . B.  $n = \Omega(n^2)$ .

**Problem 4.** Which of the following is true? Answer:

A.  $100n + \sqrt{n} + (\log_2 n)^5 = \Theta(n)$ . B.  $100n + \sqrt{n} + (\log_2 n)^5 \neq \Theta(n)$ .

**Problem 5.** Which of the following functions of n is not  $O(n^2)$ . Answer:

A.  $n^2/\log^2 n$ 

B.  $(\log_2 n)^{35}$ 

C. 100000

**Problem 6.** Which of the following functions of n is O(n). Answer:

A. 100000

B.  $n^2/\log^2 n$ 

C.  $\frac{n^{2.001}}{3583}$ 

D.  $(1.01)^n$ 

**Problem 7.** Which of the following functions of n is  $\Omega(n)$ . Answer:

A. 100000

B.  $n/\log^2 n$ 

C.  $n^{0.999}$ 

D.  $(1.01)^n$ 

**Problem 8.** Which of the following functions of n is  $not \Theta(n \log n)$ . Answer: [

A.  $35n \log_2 n + \sqrt{n}$  B.  $n \log_{35} n$  C.  $n^{1.81} + n \log_2 n$ 

D.  $n^{0.99} + 87n \log_{200} n$ .

**Problem 9.** Which of the following statements is true? Answer:

A. The running time of binary search (performed on a sorted array of n integers) is  $O(\log^2 n)$ .

B. The running time of binary search (performed on a sorted array of n integers) is O(1).

C.  $35n + \sqrt{n} = \Theta(n^2)$ .

D. In the RAM model, the time complexity of an algorithm depends on how fast a CPU is (the complexity on a 2 GHz CPU may be different from that on a 1 GHz one).

**Problem 10.** Prove  $10n + n^{1/3} = O(n)$ .

## COMP7505: Quiz 1

Name:

Student ID:

This is the quiz paper for COMP7505. If you are registered for COMP3506, turn overleaf.

Problems 1-8 bear 10 marks each. Problem 9 bears 20 marks.

**Problem 1.** Which of the following is true? Answer: [ A.  $n \log_2 n = O(n)$ . B.  $n = O(n \log n)$ .

**Problem 2.** Which of the following is true? Answer: [ ] A.  $100n + \sqrt{n} + (\log_2 n)^5 = \Theta(n)$ . B.  $100n + \sqrt{n} + (\log_2 n)^5 \neq \Theta(n)$ .

**Problem 3.** Which of the following functions of *n* is *not*  $O(n^2)$ . Answer: [ A.  $n^2/\log^2 n$  B.  $(\log_2 n)^{35}$  C. 100000 D.  $\frac{n^{2.001}}{3583}$  E.  $\frac{n^3}{2^n}$ 

**Problem 4.** Which of the following functions of n is O(n). Answer: [ A. 100000 B.  $n^2/\log^2 n$  C.  $\frac{n^2 \cdot 001}{3583}$  D.  $(1.01)^n$  E.  $n \log_2 n$ 

**Problem 5.** Which of the following functions of n is  $\Omega(n)$ . Answer: [ A. 100000 B.  $n/\log^2 n$  C.  $n^{0.999}$  D.  $(1.01)^n$  E.  $(\log_2 n)^{35}$ 

**Problem 6.** Which of the following functions of n is  $not \Theta(n \log n)$ . Answer: [A.  $35n \log_2 n + \sqrt{n}$  B.  $n \log_{35} n$  C.  $n^{1.81} + n \log_2 n$  D.  $n^{0.99} + 87n \log_{200} n$ .

**Problem 7.** Which of the following statements is true? Answer: [

- A. The running time of binary search (performed on an array of n integers) is  $O(\log^2 n)$ .
- B. The running time of binary search (performed on an array of n integers) is O(1).
- C.  $35n + \sqrt{n} = \Theta(n^2)$ .

D. In the RAM model, the time complexity of an algorithm depends on how fast a CPU is (the complexity on a 2 GHz CPU may be different from that on a 1 GHz one).

**Problem 8.** Prove  $10n + n^{1/3} = O(n)$ .

**Problem 9.** Let f(n) and g(n) be two functions of integer n. Prove: if f(n) = O(g(n)), then  $\frac{f(n)}{g(n)} = O(1)$ .