## BMEG3120: Exercise List 10

Consider the set $F$ of following functional dependencies on relation $R(A B C D E)$ :

$$
\begin{aligned}
A B & \rightarrow C \\
B C & \rightarrow E \\
B D & \rightarrow E \\
C & \rightarrow B \\
D & \rightarrow A
\end{aligned}
$$

Answer the following questions.
Problem 1. Can we simplify $F$ into the following set of FDs?

$$
\begin{aligned}
A & \rightarrow C \\
B C & \rightarrow E \\
B D & \rightarrow E \\
C & \rightarrow B \\
D & \rightarrow A
\end{aligned}
$$

Answer. No, because $A^{+}=\{A\}$ according to $F$, but $A^{+}=\{A, C\}$ in the above set of FDs.
Problem 2. Is $R$ in 3NF?
Answer. The following table shows the closures of all attribute sets (if an attribute set is not shown, its closure is $\{A, B, C, D, E\})$ :

| attribute set | closure |
| ---: | :--- |
| $A$ | $A$ (short form for $\{A\}$ ) |
| $B$ | $B$ |
| $C$ | $B C E$ |
| $D$ | $A D$ |
| $E$ | $E$ |
| $A B$ | $A B C E$ |
| $A C$ | $A B C E$ |
| $A D$ | $A D$ |
| $A E$ | $A E$ |
| $B C$ | $B C E$ |
| $B D$ | $A B C D E$ |
| $B E$ | $B E$ |
| $C D$ | $A B C D E$ |
| $C E$ | $B C E$ |
| $D E$ | $A D E$ |
| $A B C$ | $A B C E$ |
| $A B E$ | $A B C E$ |
| $A C E$ | $A B C E$ |
| $A D E$ | $A D E$ |
| $B C E$ | $B C E$ |
| $A B C E$ | $A B C E$ |

The underlined in the above table are candidate keys. $R$ is not in 3NF due to (for example) $D \rightarrow A$.

Problem 3. Compute a minimal cover of $F$.
Answer.

$$
\begin{aligned}
A B & \rightarrow C \\
C & \rightarrow B \\
C & \rightarrow E \\
D & \rightarrow
\end{aligned}
$$

Problem 4. Decompose $R$ into 3NF tables.
Answer. We first decompose $R$ into BCNF tables: $R_{1}(A C), R_{2}(A D), R_{3}(B C)$ and $R_{4}(B D E)$. Since $A B \rightarrow C$ and $C \rightarrow E$ have not been preserved in any of the tables, we add: $R_{5}(A B C)$ and $R_{6}(C E)$. The final design therefore contains: $R_{2}, R_{4}, R_{5}$ and $R_{6}$. Note that $R_{1}$ and $R_{3}$ are no longer needed because they are already contained by $R_{5}$.

