# CSCI5020 External Memory Data Structures: Exercise Spoilers

## 1 Exercise 1

**Problem 1.** Do external sort except that, in merging, combine tuples with identical keys. Argue that the cost is as desired.

**Problem 2.** Apply the algorithm we discussed for  $f = \sqrt{M/B}$  recursively.

**Problem 3.** Argue that there are  $n!/((n/k)!)^k$  different results.

#### 2 Exercise 2

**Problem 1.** Divide  $\mathbb{R}^2$  into  $\sqrt{M/B}$  slabs. They define  $\Theta(M/B)$  multi-slabs, where each multi-slab spans a number of consecutive slabs. Maintain a linked list for each multi-slab during the sweeping process.

**Problem 2.** First solve the special case where each rectangle  $r \in R$  has the form  $(-\infty, x] \times (-\infty, y]$ .

## 3 Exercise 3

Problem 1. Persistent B-tree.

Problem 2. Persistent B-tree.

**Problem 3.** Store something along with each routing element.

Problem 4. How much footprint does each update leave in your structure to the above problem?

### 4 Exercise 4

Problem 1. First build the base tree and then the secondary structures top-down.

**Problem 2.** Use a B-tree to index all the data rays by their y-coordinates, and store additional information at each routing element.

Problem 3. Persistent B-tree and filtering search.

**Problem 4.** Solution to Problem 3 and external interval tree.

#### 5 Exercise 5

**Problem 1.** Use a B-tree of branching parameter  $O((\frac{n}{B})^{1/3} \frac{1}{\log_B n}))$ , and then apply the idea of the external range tree.

Problem 2. Generalize the above idea.

**Problem 3.** First come up with a structure of O(n/B) + nL/B space with query cost  $O(\sqrt{nL/B} + kL/B)$ . Then think how to recurse.

Problem 4. Top-down.