Linked Lists, Stacks, and Queues

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A data structure has two functionalities:

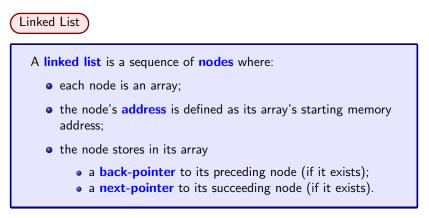
- store a set of elements;
- supports certain operations on those elements.

The only data structure in our discussion so far is the array.

In this lecture, we will first discuss a new data structure, the **linked list**, and then utilize it to design two other structures: the **stack** and the **queue**.

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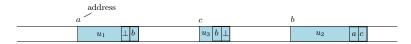
Recall that a "pointer" is a memory address.

In a linked list, the first node is called the **head** and the last node is called the **tail**.

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Linked List

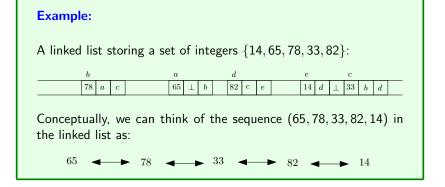
The figure below illustrates a linked list of three nodes u_1 , u_2 , and u_3 , whose addresses are *a*, *b*, and *c*, respectively.



The back-pointer of node u_1 (the head) is nil, denoted by \perp . The next-pointer of u_3 (the tail) is also nil.

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Two (Simple) Facts

Suppose that we use a linked list to store a set S of n integers (one node per integer).

Fact 1: The linked list uses O(n) space, namely, O(n) memory cells.

Fact 2: Starting from the head node, we can enumerate all the integers in S in O(n) time.

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A linked list storing a set *S* supports **updates**:

- **insertion**: add a new element to *S*;
- **deletion**: remove an existing element from *S*.

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Insertion in a Linked List

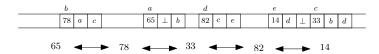
To insert a new element *e*, append *e* to the linked list:

- Identify the tail node u.
- 2 Create a new node u_{new} to store *e*.
- Set the next-pointer of u to the address of u_{new} .
- Set the back-pointer of u_{new} to the address of u.

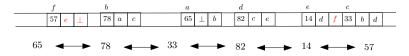
O(1) time.

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After inserting 57:



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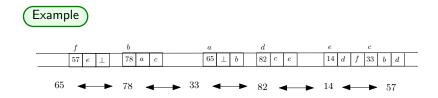
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Deletion from a Linked List

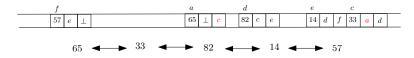
Given a pointer to a node u in the linked list, we can delete the node as follows:

- **1** Identify the preceding node u_{prec} of u.
- 2 Identify the succeeding node u_{succ} of u.
- Set the next-pointer of u_{prec} to the address of u_{succ} .
- Set the back-pointer of u_{succ} to the address of u_{prec} .
- So Free up the memory of *u*.

O(1) time



After deleting 78:



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Next, we will deploy the linked list to implement two data structures: stack and queue.

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A stack manages a set S of elements and supports two operations:

- push(e): insert a new element e into S.
- pop: remove the **most recently inserted** element from S and returns it.

First-In-Last-Out (FILO).

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Example

Consider the following sequence of operations on an empty stack:

- Push(35): $S = \{35\}.$
- Push(23): $S = \{35, 23\}.$
- Push(79): $S = \{35, 23, 79\}.$
- Pop: return 79 after removing it from S. Now $S = \{35, 23\}$.
- Pop: return 23 after removing it from S. Now $S = \{35\}$.
- Push(47): $S = \{35, 47\}.$
- Pop: return 47 after removing it from S. Now $S = \{35\}$.

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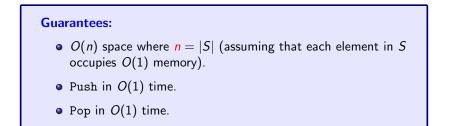
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Store the elements of S in a linked list L.

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Push(e): insert e at the end of L.
Pop: delete the tail node of L and return the element therein.
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At all times, keep track of a pointer to the tail node.





A **queue** stores a set S of elements and supports two operations:

- en-queue(e): inserts an element e into S.
- de-queue: removes the **least recently inserted** element from *S* and returns it.

First-In-First-Out (FIFO).

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Example

Consider the following sequence of operations on an initially empty queue:

- En-queue(35): $S = \{35\}$.
- En-queue(23): $S = \{35, 23\}.$
- En-queue(79): $S = \{35, 23, 79\}.$
- De-queue: return 35 after removing it from S. Now $S = \{23, 79\}$.
- De-queue: return 23 after removing it from S. Now $S = \{79\}$.
- En-queue(47): $S = \{79, 47\}.$
- De-queue: return 79 after removing it from S. Now $S = \{47\}$.

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Store the elements of S in a linked list L.

En-queue(e): insert e at the end of L. De-queue: delete the head node of L and return the element therein.

At all times, keep track of the addresses of the head and the tail.

