## CSCI2100: Special Exercise Set 11

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Problem 1. Consider the following directed graph.


Show a BFS-tree that can possibly produced by running the BFS algorithm starting from $a$.
Problem 2. Consider the graph in Problem 3. Is the following a possible order of the vertices visited (i.e., discovered) by any BFS execution?

$$
d, e, c, g, f, a
$$

Problem 3. Consider that we run BFS on the graph in Problem 1, starting from vertex $a$. Show the content of the queue at the moment right after node $g$ enters the queue.
Problem 4. Let $G=(V, E)$ be a directed graph, given in the adjacency list format. Define a directed graph $G^{\prime}=\left(V, E^{\prime}\right)$ where an edge $(u, v) \in E^{\prime}$ if and only if $(v, u) \in E$ (namely, $G^{\prime}$ reverses the direction of each edge in $G$ ). Describe an algorithm to obtain an adjacency list representation of $G^{\prime}$ in $O(|V|+|E|)$ time.

