

# SDM-PEB: Spatial-Depthwise Mamba for Enhanced Post-Exposure Bake Simulation

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# Outline

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- 2 Framework
- 3 Experiment



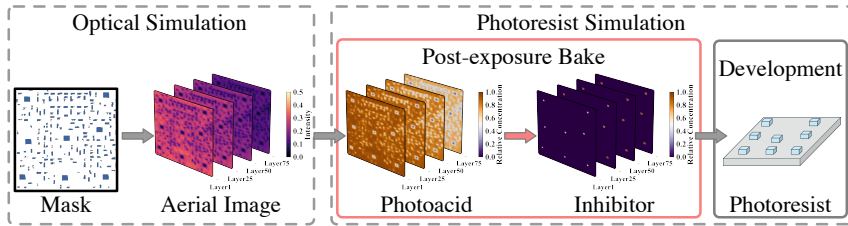
# Introduction



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# Typical Lithography Simulation Flow



A typical flow of lithography simulation for chemically amplified resist: from optical simulation to photoresist simulation.

- **Optical simulation:** light exposure process
- **Photoresist simulation:** chemical and physical processes occurring within photoresist layer



## Post Exposure Bake Process

Step 1: incident light decomposes photoacid generators, generating photoacid ( $\mathcal{A}$ ).

Step 2: photoacid catalyzed inhibitor ( $\mathcal{I}$ ) decomposition:

$$\frac{\partial[\mathcal{I}]}{\partial t} = -k_c[\mathcal{I}][\mathcal{A}], \quad (1)$$

Step 3: photoacid-base quencher( $\mathcal{B}$ ) neutralization & diffusion:

$$\frac{\partial[\mathcal{A}]}{\partial t} = -k_r[\mathcal{A}][\mathcal{B}] + D_{\mathcal{A}}\nabla^2[\mathcal{A}], \quad (2)$$

$$\frac{\partial[\mathcal{B}]}{\partial t} = -k_r[\mathcal{A}][\mathcal{B}] + D_{\mathcal{B}}\nabla^2[\mathcal{B}]. \quad (3)$$

$k_c$ : catalysis coefficient;  $k_r$ : reaction coefficient;  $D_{\mathcal{A}}, D_{\mathcal{B}}$ : the diffusion coefficients

# Development Process

Step 4: photoresist developed at a rate  $R$ :

$$R(x, y, z) = R_{max} \frac{(a + 1)(1 - [I])^n}{a + (1 - [I])^n} + R_{min}, \quad a = (1 - M_{th})^n \frac{n + 1}{n - 1}. \quad (4)$$

$R_{max}, R_{min}$ : maximum (fully exposed) and minimum (unexposed) development rates;

$n$ : surface reaction order

# Importance of Improving PEB simulation

- ① Accounts for 30% of the runtime in Synopsys Sentaurus Lithography (S-Litho)
- ② Early Methods: significant computational burden
  - Simplified reaction-diffusion equations
  - 3D diffusion profile simulations
  - Finite element analysis
  - Finite difference methods
- ③ DeePEB-Fourier Neural Operator (FNO) + CNN: Fails to capture full 3D spatial-depth dependencies; information loss in frequency segmentation

**Motivation:** Fully capture the spatial and depthwise dependencies inherent in complex physical and chemical reactions.



# Framework



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# Our Contributions

## ① Hierarchical Contextual Feature Extractor

- designed to capture both coarse and fine-grained spatial features at each depth level

## ② Spatial-Depthwise Mamba-based Attention Unit

- developed to model cross-depth-level dependencies effectively.

## ③ Customized PEB Optimization Objectives

- efficiently guide the optimization.

# Hierarchical Contextual Feature Extractor

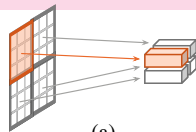
## 1. Depthwise Overlapped Patch Merging

- Reduce information loss at patch boundaries
- Enhance local continuity

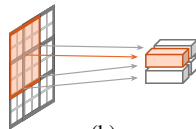
## 2. Efficient Spatial Self-Attention:

- $C$ : feature dimension of  $\mathbf{K}$ ;  $r$ : reduction ratio
- Computational complexity:  $O(L^2) \rightarrow O(L^2/r)$

$$\hat{\mathbf{K}} = \text{Reshape} \left( \frac{L}{r}, C \cdot r \right) (\mathbf{K}), \quad \mathbf{K} = \text{Linear}_C(\hat{\mathbf{K}}), \quad (5)$$



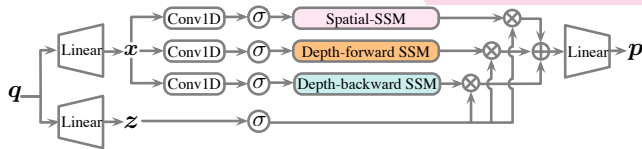
(a)



(b)

(a) Non-overlapped patch merging and (b) overlapped patch merging.

# Spatial-Depthwise Mamba-based Attention Unit



The architecture of the spatial-depthwise Mamba-based attention unit.

- 1 Feature map with dimension  $\mathbb{R}^{C_i \times D \times H_i \times W_i}$  reshaped into:  $q_i \in \mathbb{R}^{C_i \times DH_i W_i}$ .
- 2  $q_i$  linearly projected into  $x_i$  and  $z_i$  with hidden dimension  $C_i^h$ .
- 3 In each direction  $d$ :  $x_i \rightarrow$  1D convolution  $\rightarrow$  SiLU activation  $\rightarrow d$ -direction spatial-depthwise PEB selective scan
- 4 Weighted and combined to produce feature map  $p$

# Spatial-Depthwise PEB Selective Scan

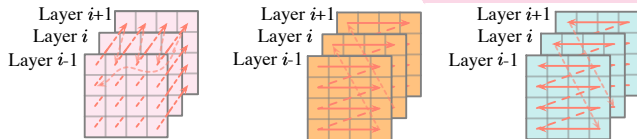


Illustration of the three-direction PEB selective scan, from left to right: spatial scan, depth-forward scan, and depthbackward scan.

- **Spatial Scan:** operates along the depth dimension to collect information at a specific spatial position across all depth layers
- **Depth-Forward Scan:** processes the entire shallow level first before transitioning to deeper levels
- **Depth-Backward Scan:** processes deeper levels before moving to shallower ones



# State Space Model

State space model (SSM):

- Capture long-range dependencies with parallel training
- Map a scalar sequence  $x(t)$  to another scalar sequence  $y(t)$  via a hidden state  $h(t) \in \mathbb{R}^N$
- $A \in \mathbb{R}^{N \times N}$ : evolution parameter;  $B, C \in \mathbb{R}^{N \times 1}$ : projection parameters

$$h'(t) = Ah(t) + Bx(t), y(t) = Ch(t). \quad (6)$$

Deep learning adaption: zero-order hold (ZOH) discretization assumption:

$$\bar{A} = \exp(\Delta A), \bar{B} = (\Delta A)^{-1}(\exp(\Delta A) - I) \cdot \Delta B, \quad (7)$$

Discretized version re-expression:

$$h_t = \bar{A}h_{t-1} + \bar{B}x_t, y_t = Ch_t. \quad (8)$$



# Mamba: Selective Scan State Space Model

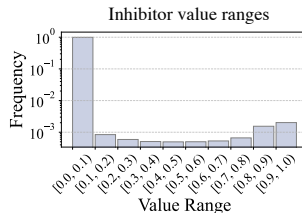
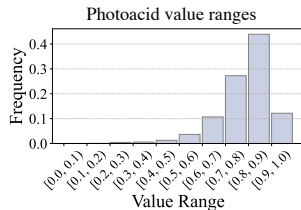
- Selectively focuses on relevant information while ignoring irrelevant inputs.
- Associate SSM projection parameters with the input
- Hardware-aware algorithm for SSM computation with linear scalability relative to sequence length
- Parallel scans: Kernel fusion and recomputation

$$\mathbf{B} = \text{Linear}_N(\mathbf{x}), \mathbf{C} = \text{Linear}_N(\mathbf{x}), \quad (9)$$

$$\Delta = \text{softplus}(\text{Broadcast}_K(\text{Linear}_1(\mathbf{x})) + \mathbf{D}), \quad (10)$$

# Customized PEB Optimization Objectives

- **Maximum squared error (MaxSE):**  $\mathcal{L}_{\text{MaxSE}} = \max_{d,h,w} \left( \hat{\mathcal{Y}}_{d,h,w} - \mathcal{Y}_{d,h,w} \right)^2$
- **PEB focal loss:**
  - distributions of both photoacid and inhibitor are highly imbalanced
  - $\mathcal{L}_{\text{PEB-FL}} = \sum_d^D \sum_h^H \sum_w^W \left| \hat{\mathcal{Y}}_{d,h,w} - \mathcal{Y}_{d,h,w} \right|^\gamma \left( \hat{\mathcal{Y}}_{d,h,w} - \mathcal{Y}_{d,h,w} \right)^2$



# Customized PEB Optimization Objectives

- **Differential depth divergence regularization:** aligning inter-layer differences
  - For every pair  $\hat{\mathcal{Y}}, \mathcal{Y} \in \mathbb{R}^{D \times H \times W}$ , calculate layer-wise forward difference maps  $\Delta\hat{\mathcal{Y}}, \Delta\mathcal{Y} \in \mathbb{R}^{(D-1) \times H \times W}$ :  $\Delta\hat{\mathcal{Y}}_d = \hat{\mathcal{Y}}_{d+1} - \hat{\mathcal{Y}}_d$ ,  $\Delta\mathcal{Y}_d = \mathcal{Y}_{d+1} - \mathcal{Y}_d$
  - convert the difference maps into probabilities to penalize high difference layers:

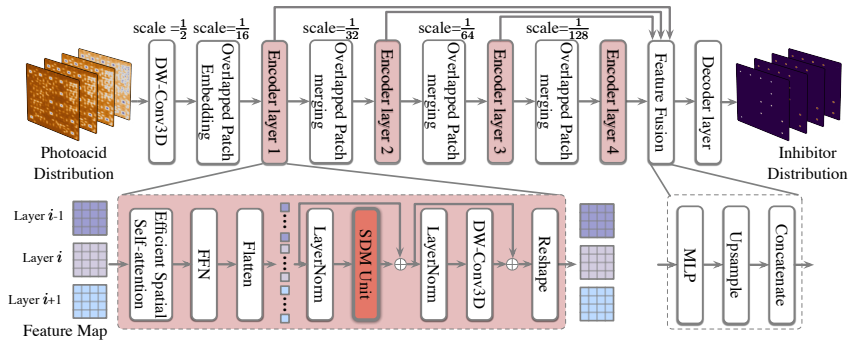
$$\sigma(\Delta\hat{\mathcal{Y}}_d) = \frac{\exp(\Delta\hat{\mathcal{Y}}_d/\tau)}{\sum_{h=1}^H \sum_{w=1}^W \exp(\Delta\hat{\mathcal{Y}}_{d,h,w}/\tau)}, \quad (11)$$

$$\sigma(\Delta\mathcal{Y}_d) = \frac{\exp(\Delta\mathcal{Y}_d/\tau)}{\sum_{h=1}^H \sum_{w=1}^W \exp(\Delta\mathcal{Y}_{d,h,w}/\tau)}, \quad (12)$$

- $\mathcal{L}_{\text{Div}}$ : Kullback-Leibler divergence between difference maps:

$$\mathcal{L}_{\text{Div}} = \sum_{d=1}^{D-1} \sigma(\Delta\hat{\mathcal{Y}}_d) \log \frac{\sigma(\Delta\hat{\mathcal{Y}}_d)}{\sigma(\Delta\mathcal{Y}_d)} \quad (13)$$

# Overall Flow



# Experiment



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# Experimental Setup

- Mask clip:  $2 \times 2 \mu m^2$  with  $80 nm$  thickness
- Resolution ( $x, y, z$ ):  $2 nm, 2 nm, 1 nm$ .
- Technology node:  $28 nm$  and below
- Simulation parameter:

**Table:** Important parameters in photoresist simulation process.

PEB			
Normal Diffusion Length $L_{N,A}, L_{N,B}$	70, 15 nm	Lateral Diffusion Length $L_{L,A}, L_{L,B}$	10, 10 nm
catalysis coefficient $k_c$	0.9 /s	reaction coefficient $k_r$	8.6993 /s
transfer coefficient $h_A, h_B$	0.027, 0	saturation concentration $[A]_{sat}, [B]_{sat}$	0.9, 0
$[T](t = 0)$	1.0	$[B](t = 0)$	0.4
Baseline Time step	0.1 s	Duration	90 s
Develop			
$R_{max}$	40 nm/s	$R_{min}$	0.0003 nm/s
$M_{th}$	0.5	n	30
Duration	60 s		

# Compare With Learning-based PEB Solvers

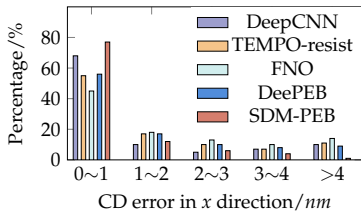
- DeepCNN: convolutional neural network model with a residual connection
- TEMPO-resist: conditional-GAN based model
- FNO: Fourier neural network
- DeePEB: extends FNO with CNN-based local learning branches

**Table:** Comparison with different PEB solvers.

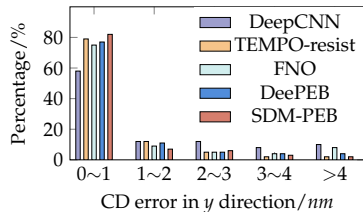
Methodologies	Inhibitor		Develop Rate		CD Error		RT/s
	RMSE ( $e-3$ )	NRMSE (%)	RMSE (nm/s)	NRMSE (%)	x (nm)	y (nm)	
DeepCNN	8.25	12.53	0.65	1.63	3.14	6.26	<b>1.01</b>
TEMPO-resist	7.67	12.55	0.50	1.26	2.12	2.45	6.48
FNO	7.91	11.68	0.68	1.69	2.34	3.71	1.15
DeePEB	3.99	5.70	0.48	1.19	0.98	1.24	1.37
SDM-PEB	<b>2.78</b>	<b>3.70</b>	<b>0.35</b>	<b>0.86</b>	<b>0.74</b>	<b>0.93</b>	1.06



# Comparison of CD Error



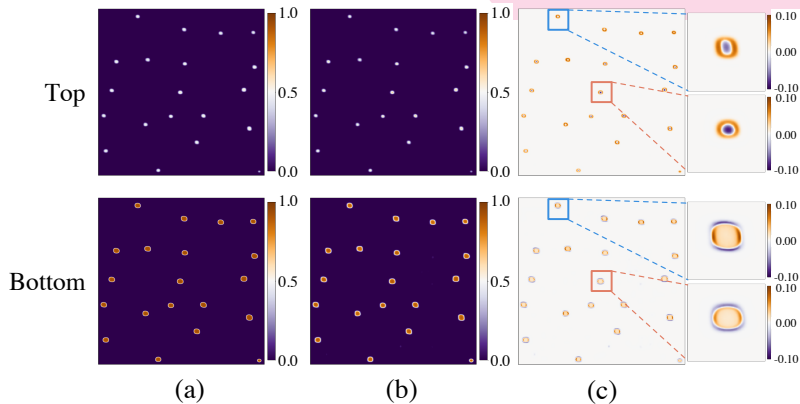
(a)



(b)

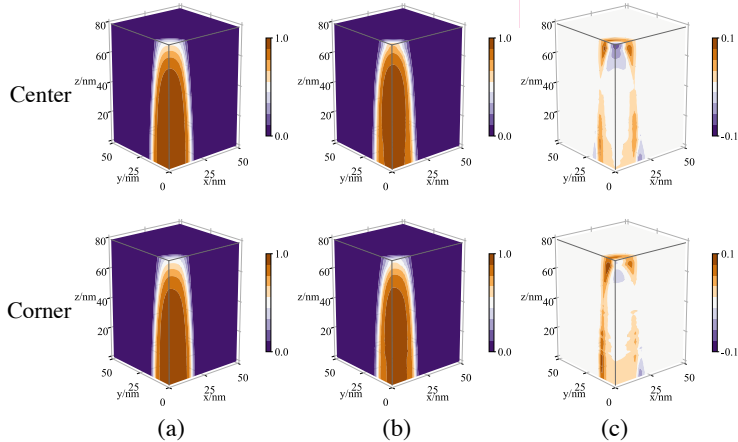
Percentage counts of CD errors using different methods: (a) error in the  $x$  direction and (b) error in the  $y$  direction.

# Visualization of Simulation Results



Top-down visualization examples of predicted distribution results. The upper row is the top surface and the lower row is the bottom surface. (a) Ground truths, (b) predictions and (c) differences.

# Visualization of Simulation Results



Vertical visualization of predicted results: the upper row shows the center contact, the lower row shows the corner contact. (a) Ground truths, (b) predictions, (c) differences.

# Ablation Study

Table: Ablation study

Methodologies	NRMSE/%		CD Error	
	Inhibitor	Rate	$x/nm$	$y/nm$
Single Layer Encoder	13.09	1.71	2.93	3.49
2-D Scan	8.83	1.58	2.07	3.05
w/o. Focal Loss	5.91	1.22	1.14	1.37
w/o. Regularization	5.98	1.24	1.15	1.42
SDM-PEB	<b>3.70</b>	<b>0.86</b>	<b>0.74</b>	<b>0.93</b>



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