## CMSC5724: Exercise List 11

Consider the mining of association rules on the transactions:

| transaction id | items |
| :---: | :--- |
| 1 | $A, B, E$ |
| 2 | $A, B, D, E$ |
| 3 | $B, C, D, E$ |
| 4 | $B, D, E$ |
| 5 | $A, B, D$ |
| 6 | $B, E$ |
| 7 | $A, E$ |

Problem 1. What is the support of the itemset $\{B, D, E\}$ ?
Problem 2. What is the support and confidence of the association rule $B D \rightarrow E$ ?
Problem 3. Consider the application of the Apriori algorithm to find all the frequent itemsets whose counts are at least 3 . Recall that the algorithm scans the transaction list a number of times, where the $i$-th scan generates the set $F_{i}$ of all size- $i$ frequent itemsets from a candidate set $C_{i}$. Show $C_{i}$ and $F_{i}$ for each possible $i$.

Problem 4. Find all the association rules with support at least 3 and confidence at least $3 / 4$. For your convenience, all the itemsets with support at least 3 are $\{\{A\},\{B\},\{D\},\{E\}$, $\{A, B\},\{A, E\},\{B, D\},\{B, E\},\{D, E\},\{B, D, E\}\}$.

Problem 5. If the universe $U$ (the set of all possible items) has size $n$, prove:

- the maximum number of distinct association rules is $\sum_{a=1}^{n-1} \sum_{b=1}^{n-a}\binom{n}{a}\binom{n-a}{b}$.
- $\sum_{a=1}^{n-1} \sum_{b=1}^{n-a}\binom{n}{a}\binom{n-a}{b}=\sum_{\ell=2}^{n}\binom{n}{\ell}\left(2^{\ell}-2\right)$.

