## CSCI3160: Quiz 3

Name:

Student ID:

**Problem 1 solution.** Independently set each variable of  $\mathcal{X}$  to 0 or 1 with equal probability.

**Problem 2 solution.**  $\{6, 7, 8\}, \{3, 4, 5\}.$ 

**Problem 3 solution:** 1.  $C^* = \{b, e\}$  and  $r(C^*) = 1$ .

2: Let  $C = \{o_1, o_2\}$  be the set returned by the k-center algorithm. Assume that  $o_1$  (or  $o_2$ , resp.) is the first (or the second, resp.) point added into C.

When  $o_1 \in \{a, b, c\}$ ,  $o_2$  must be f. We have r(C) = 2.

When  $o_1 \in \{d, e, f\}$ ,  $o_2$  must be a. We also have r(C) = 2.

Therefore, the radius of the centroid set returned by the k-center algorithm is always  $2 \cdot r(C^*)$ .