

# A Short Summary of Digital Watermarking Techniques for Multimedia Data\*

F.Y. Duan<sup>†</sup>      I. King<sup>‡</sup>

Department of Computer Science & Engineering

The Chinese University of Hong Kong

Shatin, N.T., Hong Kong, China

fyduan@letterbox.wyu.edu.cn, king@cse.cuhk.edu.hk

## Abstract

The growth of networked multimedia systems has created the need for the copyright protection of various digital medium, e.g., images, audio clips, video, etc. Copyright protection involves the authentication of ownership and the identification of illegal copies of a (possibly forged) image. One approach used to address this problem is to add a visible or invisible structure to an image that can be used to seal or mark it. These structures are known as *digital watermarks*. The watermark is capable of carrying such information as authentication or authorization codes, or a legend essential for image interpretation. This capability is envisaged to find application in image tagging, copyright enforcement, counterfeit protection, and controlled access. In this paper, we first outline the desirable characteristics of digital watermarks. Previous work in digital watermarking is then summarized. Several recent approaches that address these issues are also discussed.

## 1 Introduction

Digital media facilitate efficient distribution, reproduction, and manipulation over networked information systems for image, audio clips, and videos. However, the fact that an unlimited number of perfect copies can be illegally produced is a serious threat to the rights of content owners. However, these efficiencies also increase the problems associated with copyright enforcement. A number of technologies are being developed to provide protection from illegal copying. They include: (1) encryption methods—the use of a public and private keys to encode the data so that the image can only be decoded with the required key, (2) site security methods—the use of firewalls to restrict access, (3) using publicly accessible low quality “thumbnail” images, and (4) digital watermarking, this includes the robust unobtrusive labeling of an image with information pertaining to copyright, and the use of image checksums or other techniques to detect the manipulation of image data.

To address the non-obtrusive copyright enforcement issue, digital watermarks (i.e., author signatures) are under investigation.<sup>1</sup> Watermarking is the process of encoding hidden copyright information in an image by making small modifications to its pixel content. Unlike encryption which protects content during the transmission of the data from the sender to receiver, digital watermarking does not restrict access to the image information. Watermarking compliments encryption by embedding a signal directly into the data. Thus, the goal of a watermark is to always

---

\*This work is supported in part by RGC Earmark Grant # CUHK4176/97E.

<sup>†</sup>Research done when on-leave from Wuyi University, P.R. China.

<sup>‡</sup>Contacting author.

<sup>1</sup>Although the digital watermarking techniques described here can be applied to different multimedia medium, the majority of the techniques presented will focus more on image-related data unless stated otherwise.

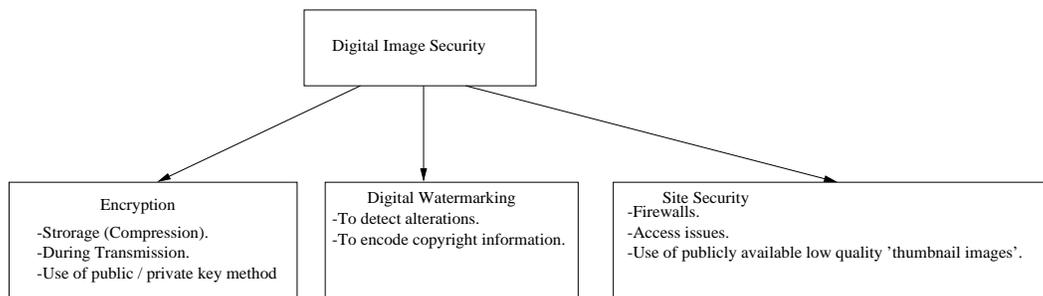


Figure 1: How Digital Watermarking Relates to Image Security Issues.

remain present in the data to provide solid proof of ownership. It should be noted that embedded signaling or watermarking can be used for a variety of other purposes other than copyright control. For example, it can be used for owner identification, to identify the content owner, fingerprinting, to identify the buyer of the content, for broadcast monitoring to determine royalty payments, and authentication, to determine whether the data has been altered in any manner from its original form. However, here we restrict our discussion here to issues that are related to copyright control.

Although there are two main divisions of watermarks, e.g., *visible* and *invisible*, this paper focuses on algorithms and techniques for invisible watermarks. In general, there are two basic requirements of invisible watermarks. The watermarks should be (1) perceptually invisible and (2) robust to common signal processing and intentional attacks. Early research on digital watermarking concentrates on the first objective without considering the second one. Recently much work has been devoted to designing robust watermarking schemes [17, 7, 23]. Perceptual models have also been incorporated to make the best tradeoff between perceptual invisibility and robustness to signal processing [23].

The goal of this paper is to give a brief summary of various digital watermarking techniques available for the purpose of authentication, forgery detection, and copyright enforcement. The paper is organized as follows. In the next section, we outline desirable properties of a watermark for copyright control, which can be quite different from watermarks for authentication purposes. Section 3 introduces a framework in which we will discuss the many different proposed watermark techniques that have been invented in recent years.

## 2 Properties of Watermarking Techniques

To be effective, the watermark should be: (1) *perceptually invisible* within the host media; (2) *statistically invisible* to thwart unauthorized removal; (3) *readily extracted* by the image owner; and (4) *robust* to accidental and intended signal distortions incurred by the host image, e.g., filtering, compression, re-sampling, re-touching, cropping, etc. These characteristics are discussed in more detail next.

### 2.1 Unobtrusive (Difficult to notice)

The watermark should be perceptually invisible to the viewer nor should the watermark degrade the quality of the content. In earlier work [7, 9, 8, 6], Cox et al., had used the term “imperceptible”, and this is certainly the ideal. However, if a signal is truly imperceptible, then perceptually-based lossy compression algorithms should, in principle, remove such a signal. Current state-of-the-art compression algorithms probably still leave room for an imperceptible signal to be inserted. This may not be true of next generation compression algorithms. Thus, to survive the next generation of lossy compression algorithms, it will probably be necessary for a watermark to be noticeable to a trained observer.

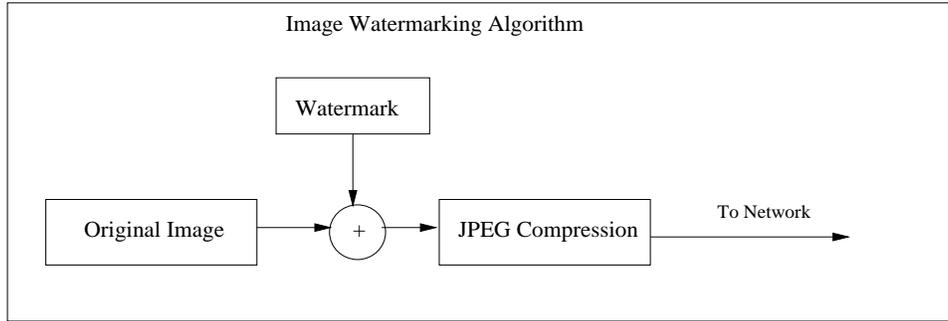


Figure 2: The schematic of image watermarking algorithm.

## 2.2 Robustness

The watermark must be difficult (hopefully impossible) to remove. Of course, in theory, any watermark may be removed with sufficient knowledge of the process of insertion. However, if only partial knowledge is available, for example, the exact location of the watermark within an image is unknown, then attempts to remove or destroy a watermark by say, adding noise, should result in severe degradation in data fidelity before the watermark is lost.

In particular, the watermark should be robust to the following attacks and characteristics.

**Universality** The same digital watermark algorithm should apply to all three media types. This is potentially helpful in the watermarking of multimedia products. Also, this feature is conducive to implementation of audio, image, and video watermarking algorithms on common hardware.

**Tamper-resistance** The watermarking techniques should be robust to legitimate signal distortions as well as intentional attacks to remove or tamper with the digital watermark.

**Common Signal Processing** The watermark should still be retrievable even if common signal processing operations are applied to the data. These include, digital-to-analog and analog-to-digital conversion, resampling, requantization (including dithering and recompression), and common signal enhancements to image contrast and color, or audio bass and treble, for example.

**Common Geometric Distortions** Watermarks in image and video data should also be immune from geometric image operations such as rotation, translation, cropping, and scaling.

**Subterfuge Attacks: Collusion and Forgery** In addition, the watermark should be robust to collusion by multiple individuals who each possess a watermarked copy of the data. That is, the watermark should be robust to combining copies of the same data set to destroy the watermarks. Further, if a digital watermark is to be used as evidence in a court of law, it must not be possible for colluders to combine their images to generate a different valid watermark with the intention of framing a third-party.

## 3 A Framework for Watermarking

A watermarking framework consists of three parts: (1) the watermark, (2) the marking algorithm, and (3) the verification algorithm. Each owner has a unique watermark which the owner would like to embed into his/her proprietary work. The marking algorithm incorporates the watermark into the multimedia medium. The verification algorithm authenticates the watermarked information, determining both the owner and the integrity of the image.

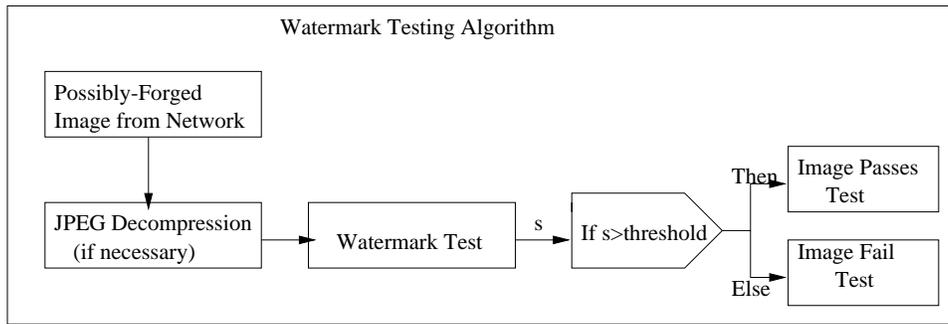


Figure 3: The schematic of watermark testing algorithm.

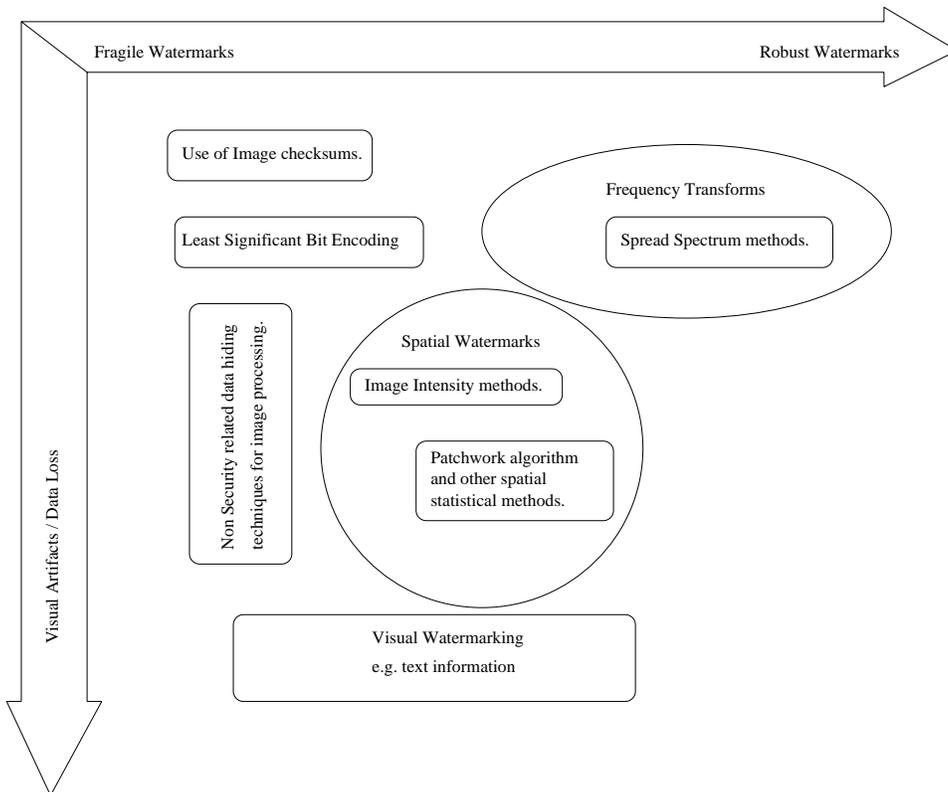


Figure 4: Classification of Digital Watermarks.

There are currently numerous techniques for applying a digital watermark to an image. The techniques can be divided into two major categories based on the desired application for the watermark (1) to detect image tampering and (2) to embed copyright information. The classification shown in Fig. 4 highlights a number of interesting characteristics of the various watermarking techniques. The techniques used to detect image tampering tend to be fragile and introduce insignificant data loss. Robust watermark algorithms used to embed copyright data tend to introduce increased visible artifacts, the notable exception are the spread spectrum methods of digital watermarking which are particularly useful for copyright labeling, being both robust and invisible. Further classification of digital watermarking can be achieved by categorizing the image data by the robustness of the watermarking technique and the obtrusiveness, the amount of visible artifacts (or data loss) introduced. With the limited scope of this paper, we will focus only on digital watermarking algorithms that embed copyright information into the targeted media.

There are several major algorithm areas with many variations. One major algorithm is based on the modification of Least Significant Bit (LSB) of the pixel content [20, 27, 28, 26]. Watermarks also can modify the image's spectral or transform coefficients directly. These algorithms often modulate Discrete Cosine Transform (DCT) coefficients according to a sequence known only to the owner [7, 13]. Watermarking techniques may be image dependent. These techniques increase the level of the watermark in the image while maintaining the imperceptibility of the mark [23, 3, 11]. For example, one of the wavelet methods incorporates features from most of the above techniques [18, 19]. Its implementation lends itself to watermarking data rate-scalable video [21]. Time stamps thwart a clever attack proposed by IBM [10] on all of these watermarking schemes. Visible watermarks also exist; IBM has developed a proprietary visible watermark to protect images that are part of the digital Vatican library project [16]. The watermarking itself is only a small part of any controlled access and distribution scheme; a method for secure distribution would combine encryption with digital watermarking [22]. Lastly there is the hybrid technique where many of these techniques may be used in combination with each other. The sections below describe these watermarking algorithms in detail.

## 3.1 Digital Watermarking Techniques

### 3.1.1 Least Significant Bit Modification

The most common and early watermarking approaches modify the least significant bits (LSB) of an image based on the assumption that the LSB data are insignificant. Two LSB techniques are described in [20]. The author first replaces the LSB of the image with a pseudo-noise(PN) sequence, while the second adds a PN sequence to the LSB of the data. And another early watermarking method obtains a checksum of the image data, then embeds the checksum into the LSB of randomly chosen pixels [26]. Others add a modified maximal length linear shift register sequence to the pixel data. They identify the watermark by using the spatial cross-correlation function of the modified sequence and part of the watermarked image [20, 27, 28].

The Digimarc Corporation describes a method that adds or subtracts small random quantities from each pixel. Addition or subtraction is determined by comparing a binary mask of  $L$  bits with the LSB of each pixel. If the LSB is equal to the corresponding mask bit, then the random quantity is added, otherwise it is subtracted. The watermark is subtracted by first computing the difference between the original and watermarked images and then by examining the sign of the difference, pixel by pixel, to determine if it corresponds to the original sequence of additions and subtractions. The Digimarc method does not make use of perceptual relevance and is probably equivalent to adding high frequency noise to the image. As such, it may not be robust to low-pass filtering.

Turner [25] proposed a method for inserting an identification string into a digital audio signal by substituting the "insignificant" bits of randomly selected audio samples with the bits of an identification code. Bits are deemed "insignificant" if their alteration is inaudible. Such a system is also appropriate for two dimensional data such as images, as discussed in [20]. Unfortunately, Turner's method may easily be circumvented. For example, if it is known that the algorithm only

affects the least significant two bits of a word, then it is possible to randomly flip all such bits, thereby destroying any existing identification code.

In a recent paper, Macq and Quisquater [14] briefly discuss the issue of watermarking digital images as part of a general survey on cryptography and digital television. The authors provide a description of a procedure to insert a watermark into the LSB of pixels located in the vicinity of image contours. Since it relies on modifications of the least significant bits, the watermark is easily destroyed. Further, their method is restricted to images, in that it seeks to insert the watermark into image regions that lie on the edge of contours.

### 3.1.2 Information Tagging

Caronni [5] suggests adding *tags* – small geometric patterns – to digitized images at brightness levels that are imperceptible. While the idea of hiding a spatial watermark in an image is fundamentally sound, this scheme is susceptible to attack by filtering and redigitization. The fainter such watermarks are the more susceptible they are such attacks and geometric shapes provide only a limited alphabet with which to encode information. Moreover, the scheme is not applicable to audio data and may not be robust to common geometric distortions, especially cropping.

Brassil et al. [4] propose three methods appropriate for document images in which text is common. Digital watermarks are coded by: (1) vertical shifting text lines, (2) horizontally shifting words, and (3) altering text features such as the vertical endlines of individual characters. Unfortunately, all three proposals are easily defeated, as discussed by the authors. Moreover, these techniques are restricted exclusively to images containing text.

### 3.1.3 Quantization Noise Embedding

Tanaka et al. [24, 15] describe several watermarking schemes that rely on embedding watermarks that resemble quantization noise. Their ideas hinge on the notion that quantization noise is typically imperceptible to viewers. Their first scheme injects a watermark into an image by using a predetermined data stream to guide level selection in a predictive quantizer. The data stream is chosen so that the resulting image looks like quantization noise. A variation on this scheme is also presented, where a watermark in the form of a dithering matrix is used to dither an image in a certain way. There are several drawbacks to these schemes. The most important is that they are susceptible to signal processing, especially requantization, and geometric attacks such as cropping. Furthermore, they degrade an image in the same way that predictive coding and dithering can.

In [24], the authors also propose a scheme for watermarking facsimile data. This scheme shortens or lengthens certain runs of data in the run length code used to generate the coded fax image. This proposal is susceptible to digital-to-analog and analog-to-digital attacks. In particular, randomizing the LSB of each pixel's intensity will completely alter the resulting run length encoding. Tanaka et al. also propose a watermarking method for "color-scaled picture and video sequences". This method applies the same signal transform as JPEG (DCT of  $8 \times 8$  sub-blocks of an image) and embeds a watermark in the coefficient quantization module. While being compatible with existing transform coders, this scheme is quite susceptible to requantization and filtering and is equivalent to coding the watermark in the least significant bits of the transform coefficients.

### 3.1.4 Statistical Techniques

Bender et al. [2] describe two watermarking schemes. The first is a statistical method called "Patchwork" that somewhat resembles the statistical component of Cox's proposal. Patchwork randomly chooses  $n$  pairs of image points,  $(a_i, b_i)$ , and increases the brightness at  $a_i$  by one unit while correspondingly decreasing the brightness of  $b_i$ . The expected value of the sum of the differences of the  $n$  pairs of points is then claimed to be  $2n$ , provided certain statistical properties of the image are true. In particular, it is assumed that all brightness levels are equally likely, that is, intensities are uniformly distributed. However, in practice, this is very uncommon. Moreover,

the scheme may (1) not be robust to randomly jittering the intensity levels by a single unit, and (2) be extremely sensitive to geometric affine transformations.

The second method is called “texture block coding”, wherein a region of random texture pattern found in the image is copied to an area of the image with similar texture. Autocorrelation is then used to recover each texture region. The most significant problem with this technique is that it is only appropriate for images that possess large areas of random texture. The technique could not be used on images of text, for example. Nor is there a direct analogy for audio.

### 3.1.5 Frequency Spectrum-Based Methods

Koch et al. [12] propose two general methods for watermarking images. The first method breaks up an image into  $8 \times 8$  blocks and computes the Discrete Cosine Transform (DCT) of each of these blocks. A pseudorandom subset of the blocks is chosen, then, in each such block, a triple of frequencies is selected from one of 18 predetermined triples and modified so that their relative strengths encode a 1 or 0 value. The 18 possible triples are composed by selection of three out of eight predetermined frequencies within the  $8 \times 8$  DCT block. The choice of the 8 frequencies to be altered within the DCT block is based on a belief that the “middle frequencies... have moderate variance”, i.e., they have similar magnitude. This property is needed in order to allow the relative strength of the frequency triples to be altered without requiring a modification that would be perceptually noticeable. Superficially, this scheme is similar to our own proposal and, in fact, also draws analogy with spread spectrum communication. However, the structure of their watermark is different from ours. The set of frequencies is not chosen based on any perceptual significance or relative energy considerations. Further, because the variance between the eight frequency coefficients is small, one would expect that their technique may be sensitive to noise or distortions. This is supported by the experimental results which report that the “embedded labels are robust against JPEG compression for a quality factor as low as about 50%”. An earlier proposal by Koch and Zhao [13] used not triples of frequencies but pairs of frequencies, and was again designed specifically for robustness to JPEG compression. Nevertheless, they state that “a lower quality factor will increase the likelihood that the changes necessary to superimpose the embedded code on the signal will be noticeably visible”.

In a second method, designed for black and white images, no frequency transform is employed. Instead, the selected blocks are modified so that the relative frequency of white and black pixels encodes the final value. Both watermarking procedures are particularly vulnerable to multiple document attacks. To protect against this, Koch and Zhao propose a distributed  $8 \times 8$  created by randomly sampling 64 pixels from the image. However, the resulting DCT has no relationship to that of the true image and consequently may be likely to cause noticeable artifacts in the image and be sensitive to noise.

### 3.1.6 Checksum Technique

This watermark is formed from the checksum value of the seven most significant bits of all pixels [26]. A checksum is the modulo-2 addition of a sequence of fixed-length binary words. It is a special type of hash function. In this technique, one word is the concatenation of eight 7-bit segments, which come from eight different pixels. Each pixel is involved in the checksum only once. The final checksum is fifty-six bits. The technique then randomly chooses the locations of the pixels that are to contain one bit of the checksum. The pixel locations of the checksum, together with the checksum itself, form the watermark. The last bit of each chosen pixel is changed (if necessary) to equal the corresponding checksum bit. This value must be kept secret. To verify this watermark the checksum of a test image is obtained, and compared to the ideal version in watermark. Any discrepancy invalidates the image. The advantages of this technique are: (1) the embedding watermark only changes (on average) half of the pixels covered by watermark, (2) an image may hold many watermarks as long as they do not overlap, and (3) this method is very fast. On the other hand, the disadvantages of this technique are: (1) this watermarking method is fragile. Any change to either the image data itself or the embedded checksum can cause the

verification procedure to fail, (2) the checksum method does not detect pixels swaps or similar attacks. A forger could replace a section with one of equal size and checksum, and (3) an attacker could remove the entire watermark by replacing the LSB plane.

### 3.1.7 Hybrid and Other Techniques

The hybrid approach combines several techniques together to synthesize a new variation of the watermarking algorithm. For example, Walton [26] uses a checksum on the image data which is embedded in the least significant bits of certain pixels. Others add a maximal length linear shift register sequence to the pixel data and identify the watermark by computing the spatial cross-correlation function of the sequence and the watermarked image [20]. Watermarks can be image dependent, using independent visual channels [11], or be generated by modulating JPEG coefficients [3]. These watermarks are designed to be invisible, or to blend in with natural camera or scanner noise. Visible watermarks also exist; IBM has developed a proprietary visible watermark to protect images that are part of the digital Vatican library project [27].

In addition to direct work on watermarking images, there are several works of interest in related areas. Adelson [1] describes a technique for embedding digital information in an analog signal for the purpose of inserting digital data into an analog TV signal. The analog signal is quantized into one of two disjoint ranges, (0, 2, 4..., 1, 3, 5..., for example) which are selected based on the binary digit to be transmitted. Thus Adelson's method is equivalent to watermark schemes that encode information into the least significant bits of the data or its transform coefficients. Adelson recognizes that the method is susceptible to noise and therefore proposes an alternative scheme wherein a  $2 \times 1$  Hadamard transform of the digitized analog signal is taken. The differential coefficient of the Hadamard transform is offset by 0 or 1 unit prior to computing the inverse transform. This corresponds to encoding the watermark into the least significant bit of the differential coefficient of the Hadamard transform. It is not clear that this approach would demonstrate enhanced resilience to noise. Furthermore, like all such least significant bit schemes, an attacker can eliminate the watermark by randomization.

## 4 Conclusion

The proliferation of network multimedia systems dictates the need for copyright protection of digital property. To conclude, any successful watermarking algorithm would have to exploit properties of the human visual system and combine these with effective modulation and channel coding. Future work will concentrate on producing watermarks that are robust to filtering, lossy image compression, noise corruption and changes in contrast. In addition these algorithms must anticipate possible attacks on the integrity and security of the watermark and to devise suitable countermeasures. This paper serves as a brief summary on several more recent and popular digital watermarking techniques for multimedia information systems.

## References

- [1] E.H. Adelson. Digital signal encoding and decoding apparatus. In *Technical Report 4,939,515, United States Patent*, 1990.
- [2] W. Bender, D. Gruhl, N. Mormoto, and A. Lu. Techniques for data hiding. *IBM Systems Journal*, 35(3):313–336, 1996.
- [3] F.M. Boland, J.J.K.O Ruanaidh, and C. Dautzenberg. Watermarking digital images for copyright protection. In *Proceedings of the International Conference on Image Processing and its Applications*, pages 321–326, Edinburgh, Scotland, July 1995.

- [4] J.T. Brassil, S. Low, N.F. Maxemchuk, and L. O’Gorman. Electronic marking and identification techniques to discourage document copying. *IEEE JOURNAL ON SELECTED AREAS IN COMMUNICATIONS*, 13(8):1495–1504, October 1995.
- [5] G. Caronni. Assuring ownership rights for digital image. In *Proc. Reliable IT Systems. VIS’95*. Vieweg Publishing Company, 1995.
- [6] I.J. Cox, J. Kilian, T. Leighton, and T. Shamoan. A secure, robust watermark for multimedia. In ed. R. Anderson, editor, *Information Hiding: First Int. Workshop Proc.*, volume 1174 of Lecture Notes in Computer Science, pages 185–206. Springer-Verlag, 1996.
- [7] I.J. Cox, J. Kilian, T. Leighton, and T. Shamoan. Secure spread spectrum watermarking for images audio and video. In *IEEE Int. Conf. on Image Processing*, volume 3, pages 243–246, Lausanne,Switzerland, September 1996.
- [8] I.J. Cox, J. Kilian, T. Leighton, and T. Shamoan. Secure spread spectrum watermarking for multimedia. *IEEE Trans. on Image Processing*, 6(12):1673–1687, 1997.
- [9] I.J. Cox and L. Miller Matt. A review of watermarking and the importance of perceptual modeling. In *Proc. of Electronic Imageing’97*, February 1997.
- [10] S. Craver, N. Memon, B.L. Yeo, and M. Yeung. Can invisible watermarks resolve rightful ownerships? In *Proceedings of the IS & T/SPIE Conference on Storage and Retrieval for Image and Video Databases V*, volume 3022, pages 310–321, San Jose, CA, USA, Feb. 13-14 1997.
- [11] J.F. Delaigle, C.D. Vleeschouwer, and B. Macq. Digital watermarking. In *Proceedings of the IS & T/SPIE Conference on Optical Security and Counterfeit Deterrence Techniques*, volume 2659, pages 99–110, San Jose, CA, USA, Feb.1-2 1996.
- [12] E. Koch, J. Rindfrey, and J. Zhao. Copyright protection for multimedia data. In *Proceedings of the Int. Conf. on Digital Media and Electronic Publishing*, 1994.
- [13] E. Koch and J. Zhao. Towards robust and hidden image copyright labeling. In *Proceedings of the 1995 IEEE Workshop on Nonlinear Signal and Image Processing*, pages 452–455, Neos Marmaras, Greece, June 20-22 1995.
- [14] B.M. Macq and J.-J. Quisquater. Cryptology for digital tv broadcasting. In *Proceedings of the IEEE*, volume 83, pages 944–957, June 1995.
- [15] K. Matsui and K. Tanaka. Video-steganography. In *IMA Intellectual Property Project Proceedings*, volume 1, pages 187–206, June 1994.
- [16] F. Mintzer, A. Cazes, F. Giordano, L. Lee, K. Magerlein, and F. Schiattarella. Capturing and preparing images of vatican library manuscripts for access via internet. In *Proceedings of the IS & T’s 48th Annual Conference*, pages 74–77, Washington,DC, May 1995.
- [17] N. Nikolaidis and I. Pitas. Copyright protection of images using robust digital signatures. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP-96)*, volume 4, pages 2168–2171, May 1996.
- [18] C.I. Podilchuk and W. Zeng. Digital image watermarking using visual models. In *IS & T/SPIE Electronic Imaging:Human Vision and Electronic Imaging*, volume 3016, Feb. 1997.
- [19] C.I. Podilchuk and W. Zeng. Watermarking of the jpeg bitstream. In *Proceeding of the International Conference on Imaging Science, Systems, and Technology*, pages 253–260, Las Vegas, Nevada,USA, June 30-July 3 1997.

- [20] R.G.van Schyndel, A.Z. Tirkel, N.R.A. Mee, and C.F. Osborne. A digital watermark. In *Proceedings of the IEEE International Conference on Image Processing*, volume 2, pages 86–90, Austin, Texas, USA, November 1994.
- [21] K. Shen and E.J. Delp. A control scheme for a data scalable video codec. In *Proceedings of the IEEE International Conference on Image Processing*, pages 69–72, Lausanne, Switzerland, September 16-19 1996.
- [22] D. Storch and E. Koch. Controlable user access on multimedia data in the world wide web. In *Proceedings of the International Conference on Imaging Science, Systems, and Technology*, pages 270–278, Las Vegas, Nevada, USA, June 30- July 3 1997.
- [23] M.D. Swanson, B. Zhu, and A.H. Tewfik. Transparent robust image watermarking. In *Proceedings of the 1996 International Conference on Image Processing*, volume 3, pages 211–214, Lausanne, Switzerland, Sept. 16-19 1996.
- [24] K. Tanaka, Y. Nakamura, and K. Matsui. Embedding secret information into a dithered multilevel image. In *Proc. 1990 IEEE Military Communications Conference*, pages 216–220, 1990.
- [25] L.T. Turner. Digital data security system. In *Patent IPN WO 89/08915*, 1989.
- [26] S. Walton. Image authentication for a slippery new age. In *Dr.Dobb's Journal*, pages 18–26, April 1995.
- [27] R.B. Wolfgang and E.J. Delp. A watermark for digital images. In *IEEE Int. Conf. on Image Processing*, volume 3, pages 219–222, Lausanne, Switzerland, 1996.
- [28] R.B. Wolfgang and E.J. Delp. A watermarking technique for digital image: further studies. In *Proceedings of the International Conference on Imaging Science, System, and Technology*, pages 279–287, Las Vegas, June 30-July 3 1997.