CENG 3420 Computer Organization & Design

Lecture 14: Cache Discussions

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(Textbook: Chapters 5.3–5.4)

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1 Example 1





4 Performance Issues



Example 1



```
short A[10][4];
int sum = 0;
int j, i;
double mean;
// forward loop
for (j = 0; j <= 9; j++)</pre>
    sum += A[j][0];
mean = sum / 10.0;
// backward loop
for (i = 9; i \ge 0; i - -)
   A[i][0] = A[i][0]/mean;
```

- Assume separate instruction and data caches
- So we consider only the data
- Cache has space for 8 blocks
- A block contains one word (byte)
- A[10][4] is an array of words located at 7A00-7A27 in row-major order

Cache Example





To simplify discussion: 16-bit word (byte) address; i.e. 1 word = 1 byte.

Direct Mapping

<u>S</u>

- Least significant 3-bits of address determine location
- No replacement algorithm is needed in Direct Mapping
- When i == 9 and i == 8, get a cache hit (2 hits in total)
- Only 2 out of the 8 cache positions used
- Very inefficient cache utilization

								Conte	nt of c	lata ca	che af	ter loo	op pas	s: (tim	e line))					
		j=0	j=1	j=2	j=3	j=4	j=5	j=6	j=7	j=8	j=9	i = 9	i = 8	i=7	i=6	i = 5	i=4	i=3	i = 2	i = 1	i = 0
	0	A[0][0]	A[0][0]	A[2][0]	A[2][0]	A[4][0]	A[4][0]	A[6][0]	A[6][0]	A[8][0]	A[8][0]	A[8][0]	A[8][0]	A[8][0]	A[6][0]	A[6][0]	A[4][0]	A[4][0]	A[2][0]	A[2][0]	A[0][0]
	1																				
	2																				
Cache	3																				
number	4		A[1][0]	A[1][0]	A[3][0]	A[3][0]	A[5][0]	A[5][0]	A[7][0]	A[7][0]	A[9][0]	A[9][0]	A[9][0]	A[7][0]	A[7][0]	A[5][0]	A[5][0]	A[3][0]	A[3][0]	A[1][0]	A[1][0]
	5																				
	6																				
	7																				

Tags not shown but are needed.

Associative Mapping

- LRU replacement policy: get cache hits for i = 9, 8, ..., 2
- If i loop was a forward one, we would get no hits!

			Content of data cache after loop pass: (time line)																		
		j=0	j = 1	j = 2	j=3	j=4	j = 5	j=6	j=7	j=8	j=9	i = 9	i = 8	i = 7	i = 6	i = 5	i = 4	i = 3	i = 2	i = 1	i = 0
	0	A[0][0]	A[0][0]	A[0][0]	A[0][0]	A[0][0]	A[0][0]	A[0][0]	A[0][0]	A[8][0]	A[0][0]										
	1		A[1][0]	A[1][0]	A[1][0]	A[1][0]	A[1][0]	A[1][0]	A[1][0]	A[1][0]	A[9][0]	A[1][0]	A[1][0]								
	2			A[2][0]																	
Cache	3				A[3][0]																
umber	4					A[4][0]															
	5						A[5][0]														
	6							A[6][0]													
	7								A[7][0]												

Tags not shown but are needed; LRU Counters not shown but are needed.



Set Associative Mapping

- Since all accessed blocks have even addresses (7A00, 7A04, 7A08, ...), only half of the cache is used, i.e. they all map to set 0
- LRU replacement policy: get hits for i = 9, 8, 7 and 6
- Random replacement would have better average performance
- If i loop was a forward one, we would get no hits!

			Content of data cache after loop pass: (time line)																		
		j=0	j=1	j=2	j=3	j=4	j= 5	j=6	j=7	j=8	j=9	i = 9	i = 8	i=7	i = 6	i = 5	i = 4	i = 3	i = 2	i = 1	i = 0
	Ó	A[0][0]	A[0][0]	A[0][0]	A[0][0]	A[4][0]	A[4][0]	A[4][0]	A[4][0]	A[8][0]	A[4][0]	A[4][0]	A[4][0]	A[4][0]	A[0][0]						
Set 0	1		A[1][0]	A[1][0]	A[1][0]	A[1][0]	A[5][0]	A[5][0]	A[5][0]	A[5][0]	A[9][0]	A[9][0]	A[9][0]	A[9][0]	A[9][0]	A[5][0]	A[5][0]	A[5][0]	A[5][0]	A[1][0]	A[1][0]
	2			A[2][0]	A[2][0]	A[2][0]	A[2][0]	A[6][0]	A[2][0]	A[2][0]	A[2][0]										
Cache	3				A[3][0]	A[3][0]	A[3][0]	A[3][0]	A[7][0]	A[3][0]	A[3][0]	A[3][0]	A[3][0]								
number	4																				
Set 1	5																				
	6																				
	7																				

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- In this example, Associative is best, then Set-Associative, lastly Direct Mapping.
- What are the advantages and disadvantages of each scheme?
- In practice,
 - Low hit rates like in the example is very rare.
 - Usually Set-Associative with LRU replacement scheme is used.
- Larger blocks and more blocks greatly improve cache hit rate, i.e. more cache memory



Example 2



How many total bits are required for a direct-mapped cache with 16 KiB of data and 4-word blocks, assuming a 32-bit address?



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Answer:

- In a 32-bit address CPU, 16 KiB is 4096 words.
- With a block size of 4 words, there are 1024 blocks.
- Each block has 4×32 or 128 bits of data plus a tag, which is (32 10 2 2) = 18 bits, plus a valid bit.
- Thus, the total cache size is $2^{10} \times (4 \times 32 + 18 + 1) = 2^{10} \times 147$ bits.
- the total number of bits in the cache is about $1.15 = \frac{147}{32 \times 4}$ times as many as needed just for the storage of the data.



How many total bits are required for an associated-mapped cache with 16 KiB of data and 4-word blocks, assuming a 32-bit address?



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Answer:

- In a 32-bit address CPU, 16 KiB is 4096 words.
- With a block size of 4 words, there are 1024 blocks.
- Each block has 4×32 or 128 bits of data plus a tag, which is (32 2 2) = 28 bits, plus a valid bit.
- Thus, the total cache size is $2^{10} \times (4 \times 32 + 28 + 1) = 2^{10} \times 157$ bits.
- the total number of bits in the cache is about $1.27 = \frac{157}{32 \times 4}$ times as many as needed just for the storage of the data.



Example 3



We have designed a 64-bit address direct-mapped cache, and the bits of address used to access the cache are as shown below:

Table: Bits of the address to use in accessing the cache

Tag	Index	Offset
63-10	9-5	4-0

- 1 What is the block size of the cache in words?
- 2 Find the ratio between total bits required for such a cache design implementation over the data storage bits.
- **3** Beginning from power on, the following byte-addressed cache references are recorded as shown below.

Table: Recored byte-addressed cache references

Hex	00	04	10	84	E8	A0	400	1E	8C	C1C	B4	884
Dec	0	4	16	132	232	160	1024	30	140	3100	180	2180

Find the hit ratio.

- Each cache block consists of four 8-byte words. The total offset is 5 bits. Three of those 5 bits is the word offset (the offset into an 8-byte word). The remaining two bits are the block offset. Two bits allows us to enumerate $2^2 = 4$ words.
- 2 The ratio is 1.21. The cache stores a total of 32lines \times 4words/block \times 8bytes/word = 1024bytes = 8192bits. In addition to the data, each line contains 54 tag bits and 1 valid bit. Thus, the total bits required is $8192 + 54 \times 32 + 1 \times 32 = 9952$ bits.
- **3** The hit ratio is $\frac{4}{12} = 33\%$

Byte Address	Binary Address	Tag	Index	Offset	Hit/Miss	Bytes Replaced
0x00	0000 0000 0000	0x0	0x00	0x00	М	
0x04	0000 0000 0100	0x0	0x00	0x04	Н	
0x10	0000 0001 0000	0x0	0x00	0x10	Н	
0x84	0000 1000 0100	0x0	0x04	0x04	М	
0xe8	0000 1110 1000	0x0	0x07	0x08	М	
0xa0	0000 1010 0000	0x0	0x05	0x00	М	
0x400	0100 0000 0000	0x1	0x00	0x00	М	0x00-0x1F
Ox1e	0000 0001 1110	0x0	0x00	0x1e	М	0x400-0x41F
0x8c	0000 1000 1100	0x0	0x04	0x0c	Н	
Oxc1c	1100 0001 1100	0x3	0x00	0x1c	М	0x00-0x1F
0xb4	0000 1011 0100	0x0	0x05	0x14	Н	
0x884	1000 1000 0100	0x2	0x04	0x04	М	0x80-0x9f



Performance Issues



Q1: Where A Block Be Placed in Upper Level?

Scheme name	# of sets	Blocks per set
Direct mapped	# of blocks	1
Set associative	# of blocks Associativity	Associativity
Fully associative	1	# of blocks



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Q2: How Is Entry Be Found?

Scheme name	Location method	# of comparisons
Direct mapped	Index	1
Set associative	Index the set; compare set's tags	Degree of associativity
Fully associative	Compare all tags	# of blocks



Q3: Which Entry Should Be Replaced on a Miss?

- Direct mapped: only one choice
- Set associative or fully associative:
 - Random
 - LRU (Least Recently Used)

Note that:

- For a 2-way set associative, random replacement has a miss rate 1.1× than LRU
- For high level associativity (4-way), LRU is too costly



Q4: What Happen On A Write?

- Write-Through:
 - The information is written in both the block in cache & the block in lower level of memory
 - Combined with write buffer, so write waits can be eliminated
 - \oplus :
 - \oplus :
- Write-Back:
 - The information is written only to the block in cache
 - The modification is written to lower level, only when the block is replaced
 - Need dirty bit: tracks whether the block is clean or not
 - Virtual memory always use write-back
 - \oplus :
 - ⊕:



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 - The information is written only to the block in cache
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 - Need dirty bit: tracks whether the block is clean or not
 - Virtual memory always use write-back
 - \oplus : write with speed of cache
 - \oplus : repeated writes require only one write to lower level



Performance

How **fast** machine instructions can be brought into the processor and how **fast** they can be executed.

- Two key factors are performance and cost, i.e., price/performance ratio.
- For a hierarchical memory system with cache, the processor is able to access instructions and data more quickly when the data wanted are in the cache.
- Therefore, the impact of a cache on performance is dependent on the hit and miss rates.



- High hit rates over 0.9 are essential for high-performance computers.
- A penalty is incurred because extra time is needed to bring a block of data from a slower unit to a faster one in the hierarchy.
- During that time, the processor is stalled.
- The waiting time depends on the details of the cache operation.

Miss Penalty

Total access time seen by the processor when a miss occurs.



Example: Consider a computer with the following parameters:

Access times to the cache and the main memory are t and 10t respectively. When a cache miss occurs, a block of 8 words will be transferred from the MM to the cache. It takes 10t to transfer the first word of the block and the remaining 7 words are transferred at a rate of one word per t seconds.

- Miss penalty = $t + 10t + 7 \times t + t$
- First t: Initial cache access that results in a miss.
- Last t: Move data from the cache to the processor.



Average Memory Access Time

 $h \times C + (1-h) \times M$

- *h*: hit rate
- M: miss penalty
- *C*: cache access time
- High cache hit rates (> 90%) are essential
- Miss penalty must also be reduced

Question: Memory Access Time Example

- Assume 8 cycles to read a single memory word;
- 15 cycles to load a 8-word block from main memory (previous example);
- cache access time = 1 cycle
- For every 100 instructions, statistically 30 instructions are data read/ write
- Instruction fetch: 100 memory access: assume hit rate = 0.95
- Data read/ write: 30 memory access: assume hit rate = 0.90

Calculate: (1) Execution cycles without cache; (2) Execution cycles with cache.





- In high-performance processors, two levels of caches are normally used, L1 and L2.
- L1 must be very fast as they determine the memory access time seen by the processor.
- L2 cache can be slower, but it should be much larger than the L1 cache to ensure a high hit rate. Its speed is less critical because it only affects the miss penalty of the L1 cache.
- Average access time on such a system:

$$h_1 \cdot C_1 + (1 - h_1) \cdot [h_2 \cdot C_2 + (1 - h_2) \cdot M]$$

- *h*₁ (*h*₂): the L1 (L2) hit rate
- *C*¹ the access time of L1 cache,
- *C*₂ the miss penalty to transfer data from L2 cache to L1
- *M*: the miss penalty to transfer data from MM to L2 and then to L1.



- Take advantage of spatial locality.
- ③ If all items in a larger block are needed in a computation, it is better to load these items into the cache in a single miss.
- © Larger blocks are effective only up to a certain size, beyond which too many items will remain unused before the block is replaced.
- ② Larger blocks take longer time to transfer and thus increase the miss penalty.
- Block sizes of 16 to 128 bytes are most popular.







Miss rate goes up if the block size becomes a significant fraction of the cache size because the number of blocks that can be held in the same size cache is smaller (increasing capacity misses)

Write buffer:

- Read request is served first.
- Write request stored in write buffer first and sent to memory whenever there is no read request.
- The addresses of a read request should be compared with the addresses of the write buffer.

Prefetch:

- Prefetch data into the cache before they are needed, while the processor is busy executing instructions that do not result in a read miss.
- Prefetch instructions can be inserted by the programmer or the compiler.

Load-through Approach

• Instead of waiting the whole block to be transferred, the processor resumes execution as soon as the required word is loaded in the cache.

