CENG 3420 Computer Organization & Design

Lecture 13: Cache

Bei Yu CSE Department, CUHK byu@cse.cuhk.edu.hk

(Textbook: Chapters 5.3–5.4)

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Overview



- 1 Introduction
- 2 Direct Mapping
- 3 Associative Mapping
- 4 Replacement
- 6 Conclusion

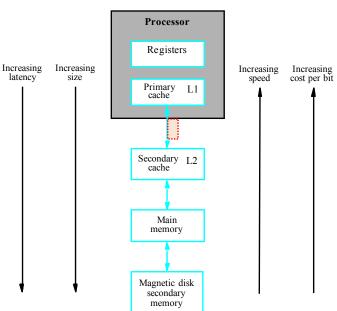


Introduction

Memory Hierarchy



- **Aim**: to produce fast, big and cheap memory
- L1, L2 cache are usually SRAM
- Main memory is DRAM
- Relies on locality of reference



Cache-Main Memory Mapping



- A way to record which part of the Main Memory is now in cache
- Synonym: Cache line == Cache block
- Design concerns:
 - Be Efficient: fast determination of cache hits/ misses
 - Be Effective: make full use of the cache; increase probability of cache hits

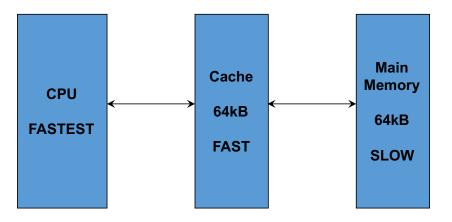
Two questions to answer (in hardware)

- Q1 How do we know if a data item is in the cache?
- Q2 If it is, how do we find it?

Imagine: Trivial Conceptual Case



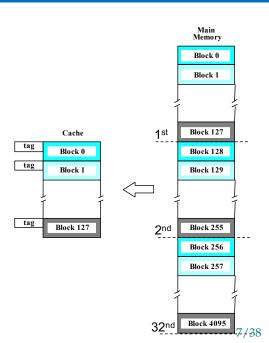
- Cache size == Main Memory size
- Trivial one-to-one mapping
- Do we need Main Memory any more?



Reality: Cache Block / Cache Line

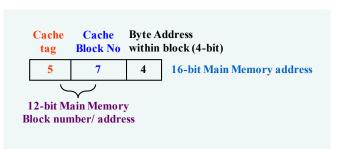


- Cache size is much smaller than the Main Memory size
- A block in the Main Memory maps to a block in the Cache
- Many-to-One Mapping

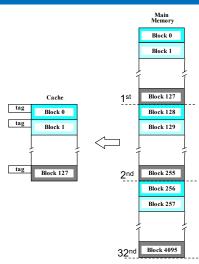


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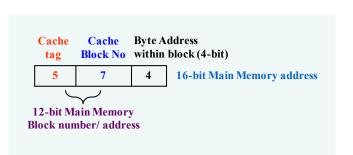




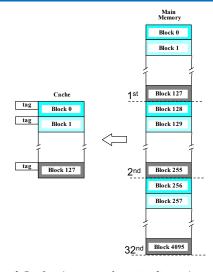
- $2^4 = 16$ bytes in a block
- $2^7 = 128$ Cache blocks
- $2^{(7+5)} = 4096$ main memory blocks







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- Block j of main memory maps to block (j mod 128) of Cache (same colour in figure)
- Cache hit occurs if tag matches desired address



Memory address divided into 3 fields

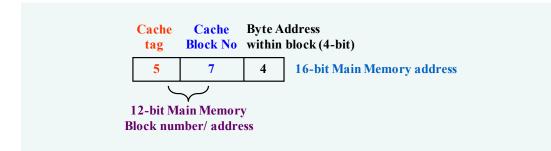
- Main Memory Block number determines position of block in cache
- Tag used to keep track of which block is in cache (as many MM blocks can map to same position in cache)
- The last bits in the address selects target word in the block

Example: given an address (t,b,w) (16-bit)

- See if it is already in cache by comparing t with the tag in block b
- 2 If not, cache miss! Replace the current block at b with a new one from memory block (t,b) (12-bit)

Direct Mapping Example 1





- **1** CPU is looking for [A7B4] MAR = **1010011110110100**
- 2 Go to cache block 1111011, see if the tag is 10100
- If YES, cache hit!
- 4 Otherwise, get the block into cache row 1111011

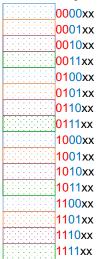
Direct Mapping Example 2



Cache

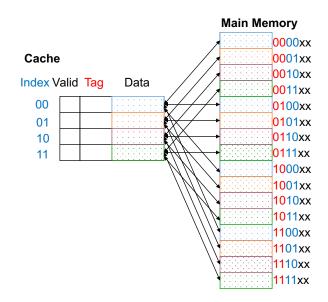
ndex V	'alid	Tag		D)2	at	:8	ì		
00					i	į	Ī	Ī	Ī	Ī
01				i	Ē	-	Ī	Ī	Ī	1
10				i	i	i	Ī	Ī	Ī	1
11			è	ì	ì	ì	ì	ì	ì	

Main Memory



Direct Mapping Example 2







Question: Direct Mapping Cache Hit Rate

Consider a 4-block empty Cache, and all blocks initially marked as not $\ \ \, \text{valid}.$ Given the main memory word addresses "0 1 2 3 4 3 4 15", calculate Cache hit rate.

Cache

Index V	alid Ta	ag Data
00		
01		
10		
11		



•	 -

00

/lem(0)	

1 miss

00	Mem(0)
00	Mem(1)

2 miss

00	Mem(0)
00	Mem(1)
00	Mem(2)

3 miss

00	Mem(0)
00	Mem(1)
00	Mem(2)
00	Mem(3)

4 miss

١1		1
' '	90	Mem(0)
	00	Mem(1)
	00	Mem(2)
	00	Mem(3)

3 hit

01	Mem(4)
00	Mem(1)
00	Mem(2)
00	Mem(3)

4 hit

01	Mem(4)
00	Mem(1)
00	Mem(2)
00	Mem(3)

15 miss

	01	Mem(4)
	00	Mem(1)
	00	Mem(2)
1	90	Mem(3)

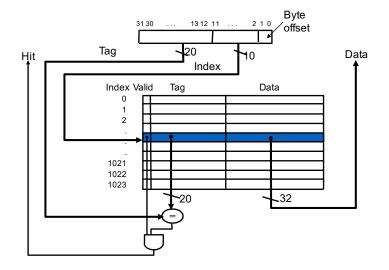
¹15

• 8 requests, 6 misses

Example 3: MIPS



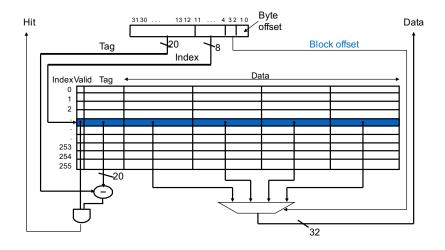
- One word blocks, cache size = 1K words (or 4KB)
- What kind of locality are we taking advantage of?



Example 4: MIPS w. Multiword Block



- Four words/block, cache size = 1K words
- What kind of locality are we taking advantage of?





Question: Multiword Direct Mapping Cache Hit Rate

Consider a 2-block empty Cache, and each block is with 2-words. All blocks initially marked as not valid. Given the main memory word addresses "0 1 2 3 4 3 4 15", calculate Cache hit rate.

Cache

ndex	Tag	Data	
00			
01			



0 miss

00 Mem(1) Mem(0)

1 hit

00 Mem(1) Mem(0)

2 miss

00 Mem(1) Mem(0) 00 Mem(3) Mem(2)

3 hit

00 Mem(1) Mem(0) 00 Mem(3) Mem(2) 4 miss

n	1	4 111133		
Ŭ	90	Mem(1)	Mem(0)	
	00	Mem(3)	Mem(2)	

3 hit

01 Mem(5) Mem(4) 00 Mem(3) Mem(2)

4 hit

01	Mem(5)	Mem(4)	
00	Mem(3)	Mem(2)	

15 miss

١	₁ 01	Mem(5)	Mem(4)
•	90	Mem(3)	Mem(2)

• 8 requests, 4 misses

Cache Field Sizes



The number of bits includes both the storage for data and for the tags

- For a direct mapped cache with 2ⁿ blocks, n bits are used for the index
- For a block size of 2^m words (2^{m+2} bytes), m bits are used to address the word within the block
- 2 bits are used to address the byte within the word

Cache Field Sizes



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Size of the tag field?

$$32-(n+m+2)$$

Cache Field Sizes



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- 2 bits are used to address the byte within the word

Size of the tag field?

$$32 - (n + m + 2)$$

Total number of bits in a direct-mapped cache

$$2^n \times (block size + tag field size + valid field size)$$



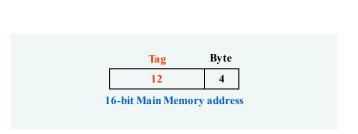
Question: Bit number in a Cache

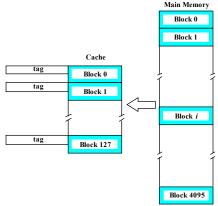
How many total bits are required for a direct mapped cache with 16KB of data and 4-word blocks assuming a 32-bit address?

Associative Mapping

Associative Mapping



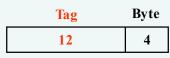




- An MM block can be in **arbitrary** Cache block location
- In this example, all 128 tag entries must be compared with the address Tag in parallel (by hardware)

Associative Mapping Example





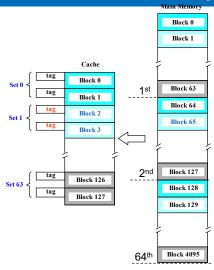
16-bit Main Memory address

- **1** CPU is looking for [A7B4] MAR = 1010011110110100
- 2 See if the tag 101001111011 matches one of the 128 cache tags
- 3 If YES, cache hit!
- 4 Otherwise, get the block into BINGO cache row

Set Associative Mapping







Combination of direct and associative

• (j mod 64) derives the Set Number

• A cache with k-blocks per set is called a k-way set associative cache.

Example: 2-way set associative

Set Associative Mapping Example 1



Tag	Set Number	Byte
6	6	4

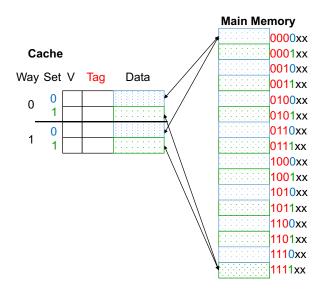
16-bit Main Memory address

E.g. 2-Way Set Associative:

- **1** CPU is looking for [A7B4] MAR = **1010011110110100**
- ② Go to cache Set 111011 (59₁₀)
 - Block 1110110 (118₁₀)
 - Block 1110111 (119₁₀)
- 3 See if ONE of the TWO tags in the Set 111011 is 101001
- 4 If YES, cache hit!
- 6 Get the block into BINGO cache row

Set Associative Mapping Example 2





Question: Direct Mapping v.s. 2-Way Set Associate



Consider the following two empty caches, calculate Cache hit rates for the reference word addresses: " $0\,4\,0\,4\,0\,4\,0\,4$ "

Cache				
Index V	alid	Tag	Data	
00				
00 01				
10				
11				
		(a)		

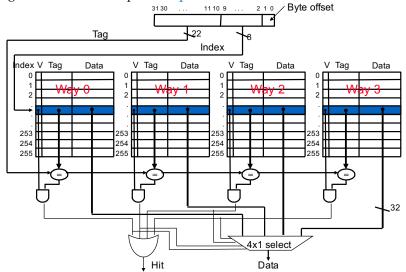
Cach	1e			
Set	Tag	Data		
0				
1				
0				
1				
(b)				

(a) Direct Mapping; (b) 2-Way Set Associative.

Set Associative Mapping Example 3: MIPS



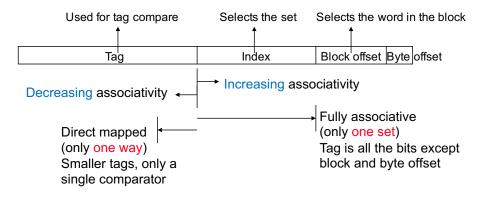
- $2^8 = 256$ sets each with four ways (each with one block).
- four tags in the set are compared in parallel.



Range of Set Associative Caches



For a fixed size cache:



Replacement

Handling Cache Read



- I\$ and D\$
- Read hit: what we want!
- Read miss: stall the pipeline, fetch the block from the next level in the memory
 hierarchy, install it in the cache and send the requested word to the processor, then let
 the pipeline resume.

Handling Cache Write Hits



Only D\$

Case 1: Write-Through

- Cache and memory to be consistent
- always write the data into both the cache block and the next level in the memory hierarchy
- Speed-up: use write buffer and stall only when buffer is full

Case 2: Write-Back

- Write the data only into the cache block
- Write to memory hierarchy when that cache block is "evicted"
- Need a dirty bit for each data cache block

Handling Cache Write Misses



Case 1: Write-Through caches with a write buffer

- No-write allocate¹
- skip cache write (but must invalidate that cache block since it now holds stale data)
- just write the word to the write buffer (and eventually to the next memory level)
- no need to stall if the write buffer isn't full

Case 2: Write-Back caches

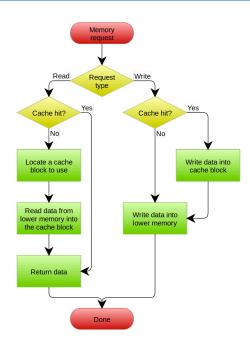
- Write allocate²
- Just write the word into the cache updating both the tag and data
- no need to stall

¹The block is modified in the main memory and not loaded into the cache.

²The block is loaded on a write miss, followed by the write-hit action.

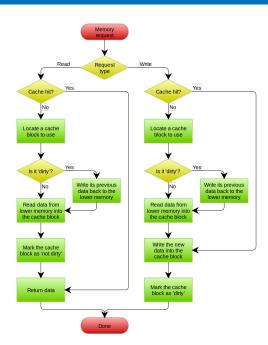
Write-Through Cache with No-Write Allocation





Write-Back Cache with Write Allocation





Replacement Algorithms



Direct Mapping

- Position of each block fixed
- Whenever replacement is needed (i.e. cache miss → new block to load), the choice is obvious and thus no "replacement algorithm" is needed

Associative and Set Associative

- Need to decide which block to replace
- Keep/retain ones likely to be used in near future again

Associative & Set Associative Replacement



Strategy 1: Least Recently Used (LRU)

- e.g. for a 4-block/set cache, use a $\log_2 4 = 2$ bit counter for each block
- Reset the counter to 0 whenever the block is accessed
- counters of other blocks in the same set should be incremented
- On cache miss, replace/ uncache a block with counter reaching 3

Associative & Set Associative Replacement



Strategy 1: Least Recently Used (LRU)

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Strategy 2: Random Replacement

- Choose random block
- ©Easier to implement at high speed

Conclusion



- Cache Organizations: Direct, Associative, Set-Associative
- Cache Replacement Algorithms: Random, Least Recently Used
- Cache Hit and Miss Penalty