Betting Odds Calculation with Machine Learning

LYU 2102

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Outline

- Introduction
- Background Knowledge
- Data Preparation
- Methodology
- Experiment and Result
- Conclusion



Introduction - Motivation

- Revenue from horse racing is approximately HK\$280 billion in 2020-2021 despite the economic downturn caused by the coronavirus pandemic
- Win odds enhance prediction accuracy as shown in previous FYP[1][2]
- Win odds keep changing before the start of the race
- Use machine learning methods to resemble the effect of winning odds in horse racing prediction

Introduction - Objective

- Apply statistical models(rating systems) to evaluate the performance of horses
- Apply techniques in natural language processing for winning horse classification
- Reproduce the effect of variable win odds from the Hong Kong Jockey Club in horse racing prediction by invariable features

Background Knowledge – Rating System

Glicko Rating System[3]

- Rating
 - Performance of a horse
- Rating deviation
 - Reliability of a horse's rating
 - a low value of rating deviation indicates that the horse joins races frequently and the rating is more reliable
 - uncertainty of a horse's ability reduces because more information is obtained when the horse joins more races



Background Knowledge – Rating System

TrueSkill Rating System[4]

- Rating
 - Performance of a horse
- Rating deviation
 - Reliability of a horse's rating
- Multiple horse environment
 - Assume outcome of each race is a permutation of multiple horses
 - Allow horses to have the same rank



Background Knowledge – Rating System

Elo-MMR Rating System[5]

- Rating
 - Performance of a horse
- Rating deviation
 - Reliability of a horse's rating
- Multiple horse environment
 - Assume outcome of each race is a permutation of multiple horses
 - Assume horses have distinct ranks
- incentive compatible
 - horses' ratings should not have opposite changes to their performance

Background Knowledge – Transformer

Self Attention mechanism[6]

- Features in the sequence interact with each other
- Assign weights to features according to the relative importance
- Decide dependency relationships between features of the sequence

Data Preparation - Collection

- Write web crawlers by using BeautifulSoup library in python
- Collect data on the HKJC official websites
- Obtain 9191 race records in our dataset dated from June 2008 to October 2021
- Obtain horse records of 6642 horses which participated in those 9191 race records

Data Preparation – Feature Analysis

- By Bayes' formula, Pr(Y = win | X = x1, x2, ...) = Pr(X = x1, x2, ... | Y = win) Pr (Y = win) / Pr (X = x1, x2, ...)
- Likelihood estimation in machine learning is simplified by assuming that features are conditional independent.
- We observe the likelihood Pr(X = x | Y = win) one by one.

Data Preparation – Feature Analysis (Age)

• Most winning horses are aged between 5 and 6



Data Preparation – Feature Analysis (Draw)

• Most winning horses have smaller draw number.



Probability of Draw Given the Winning Horse

Data Preparation – Feature Analysis (Origin)

Most winning horses come from Australia or New Zealand





Probability of Winning Given Origin

Data Preparation – Feature Analysis (Color)

• Most winning horses have skin color Bay





Data Preparation – Feature Analysis (Sex)

• Most winning horses are of sex Gelding.





Data Preparation – Feature Analysis (Numerical features)

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- Frequency of 1st place has a significant correlation with the frequency of 2nd place and 3rd place which are 0.4500 and 0.4468 respectively
- Rating systems are applicable in prediction

actual_weight -	1.0000	0.0437	-0.0043	0.0260	0.0536	0.0183	-0.0110	0.0027	-0.1565	-0.0845	
clared_weight -	0.0437	1.0000	0.0316	0.1138	0.0592	0.0246	-0.0177	-0.1547	-0.0898	-0.0586	
age -	-0.0043	0.0316	1.0000	0.6062	0.5472	0.6057	0.8560	0.1695	-0.0970	-0.0535	
1st -	0.0260	0.1138	0.6062	1.0000	0.4500	0.4468	0.6622	0.0587	-0.1882	-0.1980	
2nd -	0.0536	0.0592	0.5472	0.4500	1.0000	0.5175	0.6545	0.0592	-0.1979	-0.1839	
3rd -	0.0183	0.0246	0.6057	0.4468	0.5175	1.0000	0.6581	0.0610	-0.1868	-0.1677	
total -	-0.0110	-0.0177	0.8560	0.6622	0.6545	0.6581	1.0000	0.1732	-0.1107	-0.0607	
finish_time -	0.0027	-0.1547	0.1695	0.0587	0.0592	0.0610	0.1732	1.0000	-0.0704	0.0299	
win_odds -	-0.1565	-0.0898	-0.0970	-0.1882	-0.1979	-0.1868	-0.1107	-0.0704	1.0000	0.4291	
place -	-0.0845	-0.0586	-0.0535	-0.1980	-0.1839	-0.1677	-0.0607	0.0299	0.4291	1.0000	
	actual_weight -	declared_weight -	age	lst -	2nd -	3rd -	total -	finish_time -	win_odds -	place -	16

Data Preparation – Feature Analysis (Numerical features)

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- A positive correlation of 0.4291 between the win odds and the place
- Winning odds help the prediction of horse racing result

actual_weight -	1.0000	0.0437	-0.0043	0.0260	0.0536	0.0183	-0.0110	0.0027	-0.1565	-0.0845	
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	actual_weight -	declared_weight -	age -	lst -	2nd -	3rd -	total -	finish_time -	win_odds -	place -	17

Data Preparation – Data Imputation

- A small part of horse data about those retired horses is missing in our data set
- do data imputation on our dataset by using the k nearest neighbors method
- Invoke the KNN Imputer from Scikit Learn library to impute the missing values

Data Preparation – Data Encoding

- Input of our neural network models must be numerical but some of our data are categorical
- One hot encoding[7]
 - dimension of our input will be increased drastically
 - requires extra memory and more computational time in training
- Ordinal Encoding scheme[7]
 - a unique integer means a category
 - dimension of the data is the same as the original
- invoke the Ordinal Encoder from the Scikit Learn Library

Data Preparation – Normalization

- z-score normalization[8]
- Values of all variables are recomputed into the same scale
- the same scale of all variables balances the focus of error minimization in the weight correction algorithm

$$x_i' = \frac{x_i - \overline{x_i}}{\sigma_i}$$

Data Preparation – Rating Generation

- Ratings mentioned before do not exist on the HKJC websites
- need to calculate those ratings with the information provided by our dataset

rating mu	rating sig	perf_score	place
1400	174	1381	g
1384	133	1365	11
1481	114	1724	5
1443	102	1370	9
1463	95	1511	7
1482	90	1540	. 7
1491	87	1517	6
1522	85	1639	6
1543	84	1620	4
1563	82	1642	6
1527	82	1370	10
1562	81	1700	2
1610	81	1833	1
1613	81	1623	5
1626	80	1677	6
	rating_mu 1400 1384 1481 1443 1463 1463 1463 1482 1491 1522 1543 1563 1563 1527 1562 1610 1613 1626	rating_murating_sig1400174138413314811141443102144390146395148290148290149187152285154384156382156281161081161381	rating_murating_sigperf_score1400174138113841331365148111417241443102137014639515111482901540148290154014918715171522851639154384162015538216421563821370161481183316158116231626801677

Methodology - Overview

- Rating systems estimate the relative skill level of horses based on their historical performance
- Self attention mechanism captures the dependencies between horses
- Multiclass classification on place
 - The winning horse number is the output

Transformer classification model including ratings in the feature list

Methodology - Evaluation

- Accuracy
 - Accurate prediction about the winner
- Betting simulation
 - Net gain
 - Bet \$10 for each race in test data
- Combining transformer architecture and ratings give a better result
 - Multilayer perceptron with ratings
 - Transformer without ratings
 - Transformer with ratings

Methodology – Multilayer perceptron

- 1. Input layer
- 2. 3 linear hidden layer
- 3. Dropout layer
- 4. Output layer
- Relu Activation function
- Cross-Entropy Loss Function
- Stochastic gradient descent



Methodology – Transformer

- 1. Input layer
- 2. Word embedding layer
- 3. Position embedding layer
- 4. Transformer encoder
- 5. 2 linear hidden layers
- 6. Dropout layer
- 7. Output layer
- Relu Activation function
- Cross-Entropy Loss Function
- Stochastic gradient descent

Experiment and Result – Input Data

- Training data :
 - races from 22 June 2008 to 6 December 2020.
 - 8500 races
- Testing data
 - all races from 9 December 2020 to 17 October 2021.
 - 688 races



Experiment and Result – Input Data

Feature	Description
Venue	Location of the race
Horse_class	Class of the horses Stronger horses compete in high race class
Distance	The distance of the race
Going	Condition of the lane
Course_track	The lane of the race
Course_track_code	Description about the lane
Horse_i_number	The horse number in the race
Horse_i_name	The name of horse
Horse_i_jockey	The name of jockey
Horse_i_trainer	The name of trainer
Horse_i_declared_weight	The weight of horse
Horse_i_origin	The place of birth
Horse_i_age	The age of horse
Horse_i_color	The color of skin
Horse_i_sex	The gender of horse
Horse_i_1 st _place_frequency	The frequency of getting 1 st place
Horse_i_total_race	The total count of horse's participation
Horse_i_rating	The rating of the horse

Repeat 14 times —

Experiment and Result – Accuracy

- Multilayer perceptron with ratings
- The model with Glicko ratings reaches the highest test accuracy of 20.4%
- The accuracy of the model with Glicko ratings fluctuates in a larger range than that with Elo-MMR and TrueSkill



Experiment and Result – Accuracy

- Transformer without ratings
- the best performance of this model is having 19.2% before overfitting



Experiment and Result – Accuracy

- Transformer with ratings
- The transformer model with Elo-MMR ratings has the highest test accuracy of 21.4% among the other models



Experiment and Result – Betting Simulation

- Multilayer perceptron with ratings
- all three models perform better than random betting
- Multilayer perceptron with Elo-MMR ratings has the best performance
 - highest net gain : -13%



Experiment and Result – Betting Simulation

- Transformer without ratings
- The net gain is -4% after betting on all 688 races in our test data
- Better than the multilayer perceptron



Experiment and Result – Betting Simulation

- Transformer with ratings
- Positive net gain of 3% to 6% after betting on 688 races in the test data
- Transformer with Elo-MMR ratings has the best performance



Conclusion

- Win odds in the feature list have the effect of enhancing the accuracy and net gain
- Exclude the win odds from the feature list this time
- Resemble the effect of the winning odds by combining rating systems and the transformer architecture
- the best case of our models is the transformer with Elo-MMR ratings
 - the highest test accuracy : 21.4%
 - a positive net gain : 6%



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