

# An Energy-Efficient Mobile Recommender System

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# Outline

- Introduction
- Mobile Sequential Recommendation
- Recommending Point Generation
- LCP and SkyRoute Algorithms
- Experimental Results
- Conclusions

# Application Background

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# Research Motivation

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- Traditional recommender system
  - Prediction performance (MSE/RMSE)
  - Implicit/Explicit rating
  
- Mobile recommender system
  - Business success metrics
  - Location-based recommendation

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# Problem Formulation

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## The MSR Problem

**Given:** A set of potential pick-up points  $\mathcal{C}$  with  $|\mathcal{C}| = N$ , a probability set  $\mathcal{P} = \{P(C_1), P(C_2), \dots, P(C_N)\}$ , a directed sequence set  $\vec{\mathcal{R}}$  with  $|\vec{\mathcal{R}}| = M$  and the current position (*PoCab*) of a cab driver, who needs the service.

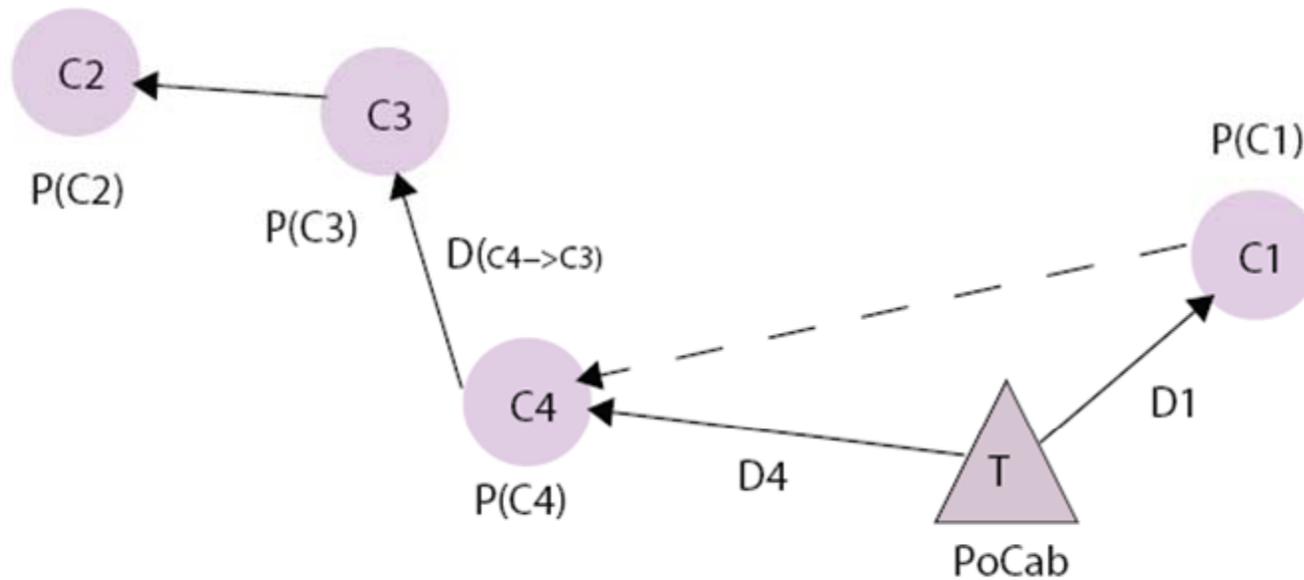
**Objective:** Recommending an optimal driving route  $\vec{\mathbb{R}}$  ( $\vec{\mathbb{R}} \in \vec{\mathcal{R}}$ ). The goal is to minimize the PTD:

$$\min_{\vec{R}_i \in \vec{\mathcal{R}}} \mathcal{F}(\text{PoCab}, \vec{R}_i, \mathcal{P}_{\vec{R}_i}) \quad (1)$$

- $\mathcal{P}_{\vec{R}_i}$ : all probabilities of all pick-up points contained in  $\vec{R}_i$
- PTD: Potential travel distance

# An Example

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An Illustration Example.

PoCab -> C1 -> C4 **or** PoCab -> C4 -> C3 -> C2?

# Two Challenges

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- Mining reliable pick-up point with probability information
- Computation challenge to search the optimal route

LEMMA 1. *Given a set of pick-up points  $C$ , where  $|C| = N$ ,  $1 \leq L_{\vec{R}_i} \leq N$  and  $Cox(\mathcal{F}) = 1$ , the complexity of searching an optimal directed sequence from  $\vec{\mathcal{R}}$  is  $\mathcal{O}(N!)$*

## The MSR Problem with a Length Constraint

**Objective:** Recommending an optimal sequence  $\vec{R}^{\mathcal{L}}$  ( $\vec{R}^{\mathcal{L}} \in \vec{\mathcal{R}}$ ). The goal is to minimize the PTD:

$$\min_{\vec{R}_i^{\mathcal{L}} \in \vec{\mathcal{R}}} \mathcal{F}(PoCab, \vec{R}_i^{\mathcal{L}}, \mathcal{P}_{\vec{R}_i^{\mathcal{L}}})$$

$\vec{R}_i^{\mathcal{L}}$  denote the recommended route with a length of  $\mathcal{L}$

Computational complexity:  $\mathcal{O}(N^{\mathcal{L}})$

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# Recommending Point Generation

- High-performance Drivers
  - Sufficient Driving Hours
  - High Occupancy Rate
- Clustering based on Driving Distance
  - Clustering close pick-up points into one pick-up cluster
- Probability Calculation
  - Ratio of Pick-up Events Happening when cab travels across pick-up clusters

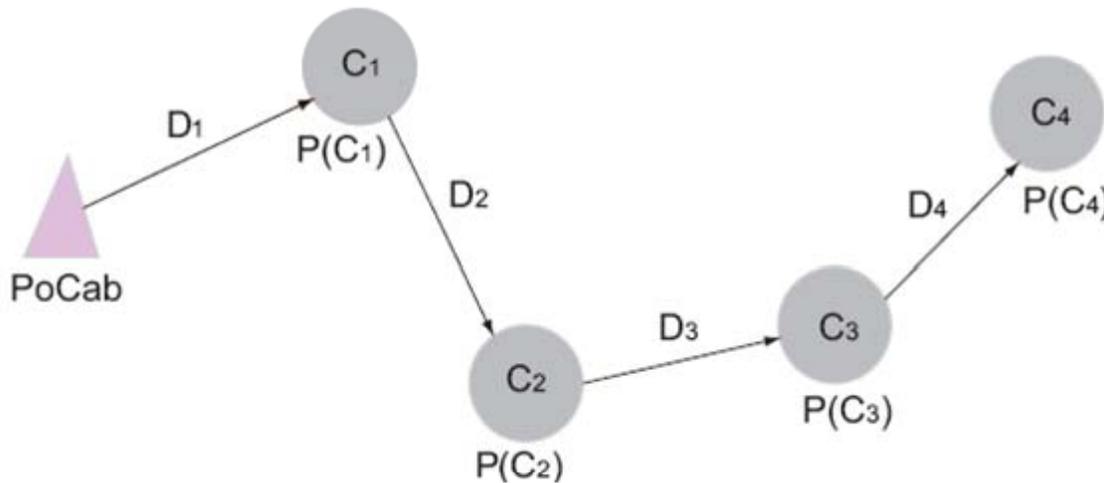
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# Potential Travel Distance

Function:  $\mathcal{F}(PoCab, \overrightarrow{R_i^{\mathcal{L}}}, \mathcal{P}_{\overrightarrow{R_i^{\mathcal{L}}}})$

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A Recommended Driving Route.

PoCab: the position of a cab  
 C1: one pick-up point  
 P(C1): the probability of pick-up event  
 D1: the driving distance

Two Vectors:

$$\mathcal{D}_{\overrightarrow{R^{\mathcal{L}}}} = \langle D_1, (D_1 + D_2), (D_1 + D_2 + D_3), (D_1 + D_2 + D_3 + D_4), D_{\infty} \rangle$$

$$\mathcal{P}_{\overrightarrow{R^{\mathcal{L}}}} = \langle P_1, \overline{P(C_1)} \cdot P(C_2), \overline{P(C_1)} \cdot \overline{P(C_2)} \cdot P(C_3), \overline{P(C_1)} \cdot \overline{P(C_2)} \cdot \overline{P(C_3)} \cdot P(C_4), \overline{P(C_1)} \cdot \overline{P(C_2)} \cdot \overline{P(C_3)} \cdot \overline{P(C_4)} \rangle$$

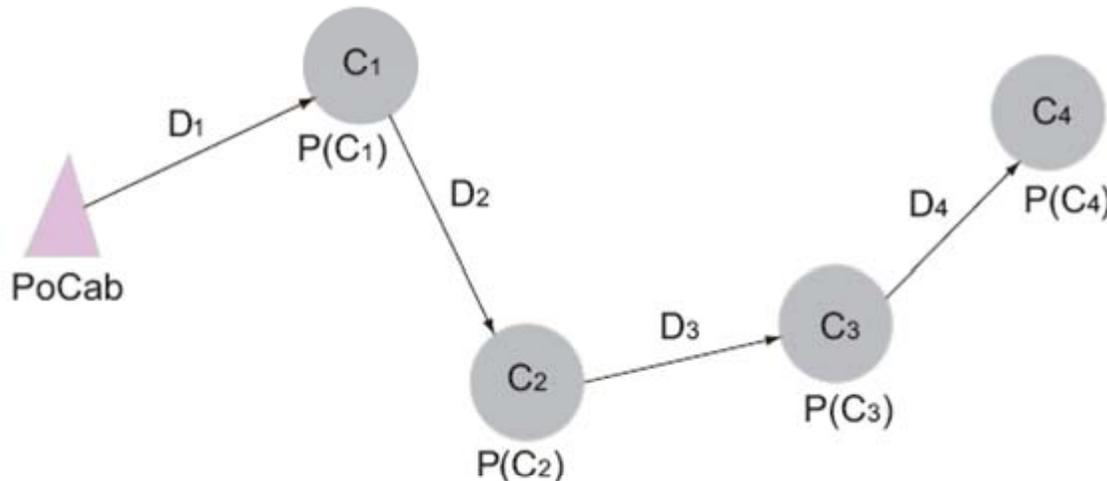
PTD Function:

$$\mathcal{F}(PoCab, \overrightarrow{R_i^{\mathcal{L}}}, \mathcal{P}_{\overrightarrow{R_i^{\mathcal{L}}}}) = \mathcal{D}_{\overrightarrow{R^{\mathcal{L}}}} \cdot \mathcal{P}_{\overrightarrow{R^{\mathcal{L}}}} \text{ where } \cdot \text{ is the dot product}$$

# Potential Travel Distance

Function:  $\mathcal{F}(PoCab, \overrightarrow{R_i^{\mathcal{L}}}, \mathcal{P}_{\overrightarrow{R_i^{\mathcal{L}}}})$

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A Recommended Driving Route.

- PoCab: the position of a cab
- C1: one pick-up point
- P(C1): the probability of pick-up event
- D1: the driving distance

One Vectors:

$$\mathcal{DP} = \langle D_1, \overline{P(C_1)}, D_2, \overline{P(C_2)}, D_3, \overline{P(C_3)}, D_4, \overline{P(C_4)} \rangle$$

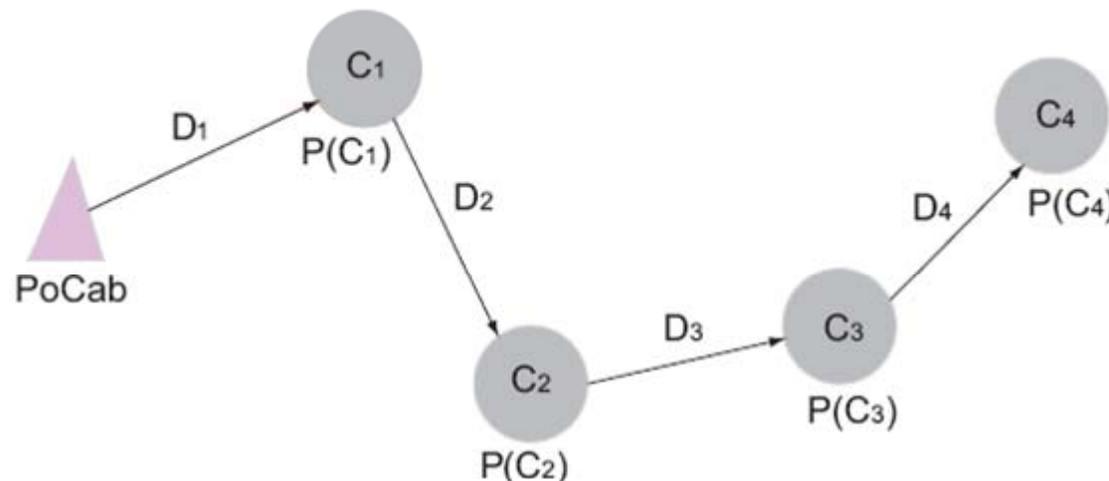
Generally, for  $\overrightarrow{R_i^{\mathcal{L}}}$ ,  $\mathcal{DP} = \langle DP_1, \dots, DP_l, \dots, DP_{2\mathcal{L}} \rangle$

PTD Function:

$$\mathcal{F}(PoCab, \overrightarrow{R_i^{\mathcal{L}}}, \mathcal{P}_{\overrightarrow{R_i^{\mathcal{L}}}}) = \mathcal{F}(\mathcal{DP})$$

# Important Property of PTD Function

**LEMMA 3. The Monotone Property of the PTD Function  $\mathcal{F}$ .** *The PTD Function  $\mathcal{F}(\mathcal{DP})$  is strictly monotonically increasing with each attribute of vector  $\mathcal{DP}$ , which is a  $2\mathcal{L}$ -dimensional vector.*



**A Recommended Driving Route.**

$$\mathcal{DP} = \langle D_1, \overline{P(C_1)}, D_2, \overline{P(C_2)}, D_3, \overline{P(C_3)}, D_4, \overline{P(C_4)} \rangle$$

# Route Dominance

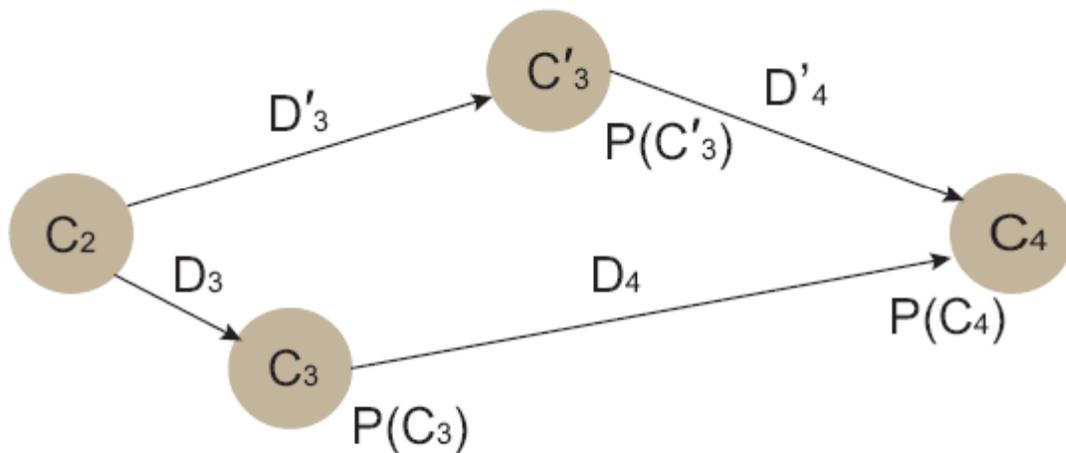
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**DEFINITION 1. Route Dominance.** *A recommended driving route  $\vec{R}^{\mathcal{L}}$ , associated with the vector  $\mathcal{DP}$ , dominates another route  $\vec{\tilde{R}}^{\mathcal{L}}$ , associated with the vector  $\vec{\tilde{\mathcal{D}\mathcal{P}}}$ , iff  $\exists 1 \leq l \leq 2\mathcal{L}, DP_l < \vec{\tilde{\mathcal{D}\mathcal{P}}}_l$  and  $\forall 1 \leq l \leq 2\mathcal{L}, DP_l \leq \vec{\tilde{\mathcal{D}\mathcal{P}}}_l$ . This can be denoted as  $\vec{R}^{\mathcal{L}} \Vdash \vec{\tilde{R}}^{\mathcal{L}}$ .*

By this definition, if a candidate route A is dominated by a candidate route B, A cannot be an optimal route

# Constrained Sub-route Dominance

**DEFINITION 2. Constrained Sub-route Dominance.**  
 Consider that two sub-routes  $\vec{R}_{sub}$  and  $\vec{R}'_{sub}$  with an equal length (the number of pick-up points) and the same source and destination points. If the associated vector of  $\vec{R}_{sub}$  dominates the associated vector of  $\vec{R}'_{sub}$ , then  $\vec{R}_{sub}$  dominates  $\vec{R}'_{sub}$ , i.e.  $\vec{R}_{sub} \Vdash \vec{R}'_{sub}$ .



$$\vec{R}_{sub} \text{ is } C_2 \rightarrow C_3 \rightarrow C_4$$

$$\vec{R}'_{sub} \text{ is } C_2 \rightarrow C'_3 \rightarrow C_4$$

$$DP_{sub} = \langle D_3, \overline{P(C_3)}, D_4, \overline{P(C_4)} \rangle$$

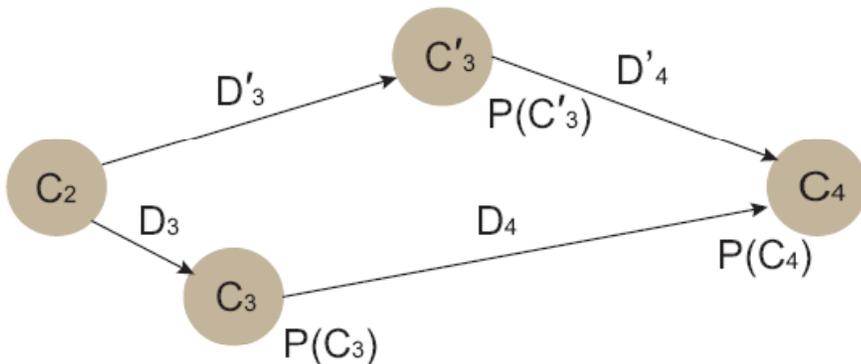
$$DP'_{sub} = \langle D'_3, \overline{P(C'_3)}, D'_4, \overline{P(C_4)} \rangle$$

Illustration: the Sub-route Dominance

# The $\mathcal{LCP}$ Algorithm

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PROPOSITION 1.  **$\mathcal{LCP}$  Pruning.** For two sub-routes  $A$  and  $B$  with a length  $\mathcal{L}$ , which includes only pick-up points, if sub-route  $A$  is dominated by sub-route  $B$  under Definition 2, the candidate routes with a length  $\mathcal{L}$  which contain sub-route  $A$  will be dominated and can be pruned in advance.



If  $\mathcal{L} = 3$  and  $\vec{R}_{sub}$  dominates  $\vec{R}'_{sub}$   
 Then  $PoCab \rightarrow C_2 \rightarrow C_3 \rightarrow C_4$   
 dominates  $PoCab \rightarrow C_2 \rightarrow C'_3 \rightarrow C_4$

- ◆ Enumerate all sub-routes with length of  $L$
- ◆ Prune dominated constrained sub-routes with length of  $L$
- ◆ Once effort to prune search space offline

# Skyline Route

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**DEFINITION 3. Skyline Route.** *A recommended driving route  $\vec{R}^{\mathcal{L}}$  is a skyline route iff  $\forall \vec{R}_i^{\mathcal{L}} \in \vec{\mathcal{R}}, \vec{R}_i^{\mathcal{L}}$  cannot dominate  $\vec{R}^{\mathcal{L}}$  by Definition 1. This is denoted as  $\vec{R}_i^{\mathcal{L}} \not\prec \vec{R}^{\mathcal{L}}$ .*

**LEMMA 4. Joint Principle of Skyline Routes and the PTD Function  $\mathcal{F}$ .** *The optimal driving route determined by the PTD function  $\mathcal{F}$  should be a skyline route. This is denoted as  $\vec{R}^{\mathcal{L}} \in \vec{\mathcal{R}}_{\text{Skyline}}$*

- ◆ First find the skyline routes
- ◆ Search the optimal driving route from the set of skyline routes

# The SkyRoute Algorithm

- Traditional Skyline computing algorithms
  - time-consuming and large memory
- Pruning for SkyRoute
  - Prune some candidates including dominated sub-routes, at a very early stage
  - The search space will be significant reduced, since lots of candidates containing dominated sub-routes are discarded
  - Gradual effort to continue prune the search space

# One Pruning Illustration

- If **SubRoute  $R_1$**  ( $\text{PoCab} \rightarrow C_1 \rightarrow C_3$ ) dominates **SubRoute  $R_2$**  ( $\text{PoCab} \rightarrow C_2 \rightarrow C_3$ )  
by **DEFINITION 2**

Then **Any candidate** like

( $\text{PoCab} \rightarrow C_1 \rightarrow C_3 \rightarrow C_i \rightarrow \dots \rightarrow C_L$ ) dominates  
**candidate as**

( $\text{PoCab} \rightarrow C_2 \rightarrow C_3 \rightarrow C_i \rightarrow \dots \rightarrow C_L$ ),

where  $C_i \rightarrow \dots \rightarrow C_L$  is one of all possible sub-routes

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# Experimental Setup

## □ Data set

### □ Real data set:

- 500+ taxi drivers, 30 days, San Francisco Bay Area
- Time period: 2-3PM, 6-7PM
- 10 pick-up clusters

### □ Synthetic data set: 10, 15, 20 Pick-up points

## □ Platform

- Intel Core2 Quad Q8300 and 6.00GB RAM
- Windows 7 Professional
- Matlab 2008a

# An Illustration of Optimal Driving Route

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◆ 6-7PM

◆  $L=3$ :

$PoCab \rightarrow C1 \rightarrow C3 \rightarrow C2$

◆  $L=4$ :

$PoCab \rightarrow C1 \rightarrow C3 \rightarrow C2 \rightarrow C7$

◆  $L=5$

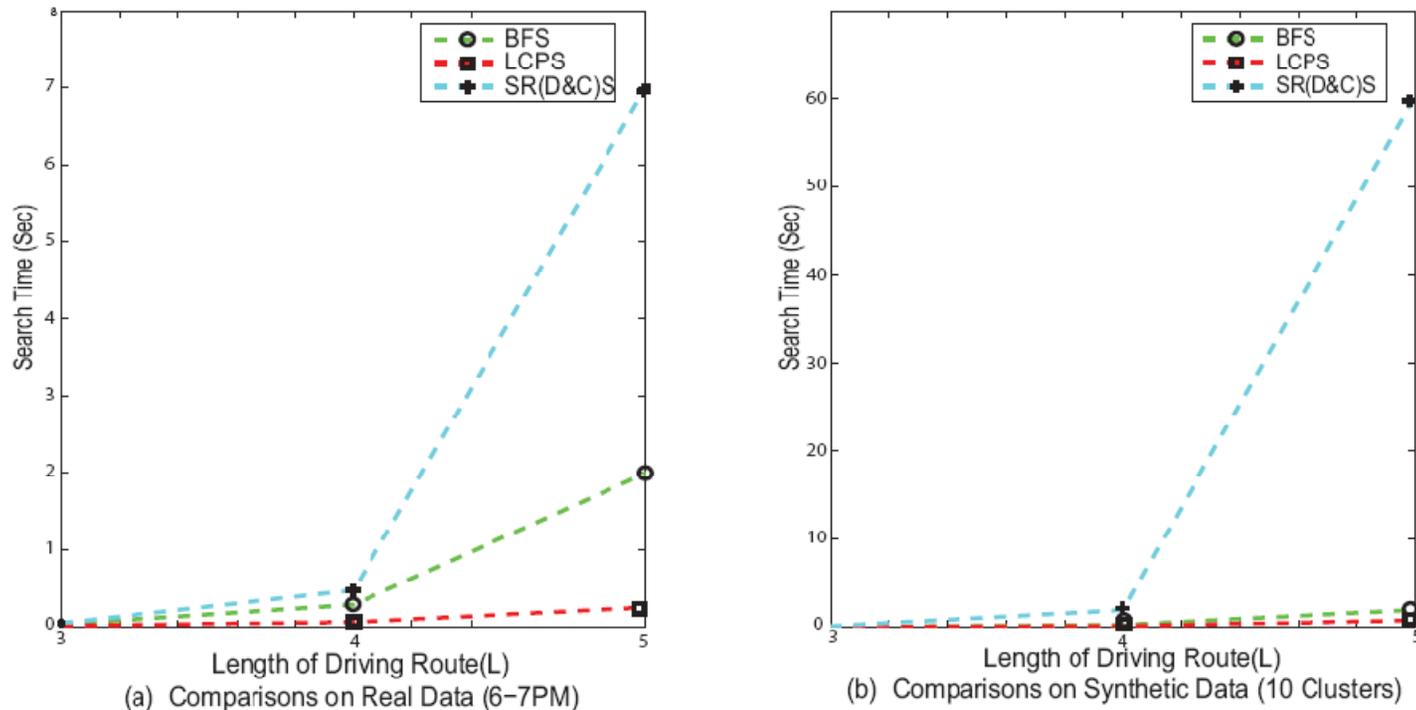
$PoCab \rightarrow C4 \rightarrow C1 \rightarrow C3 \rightarrow C2 \rightarrow C7$



# An Overall Comparison

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## A Comparison of Search Time



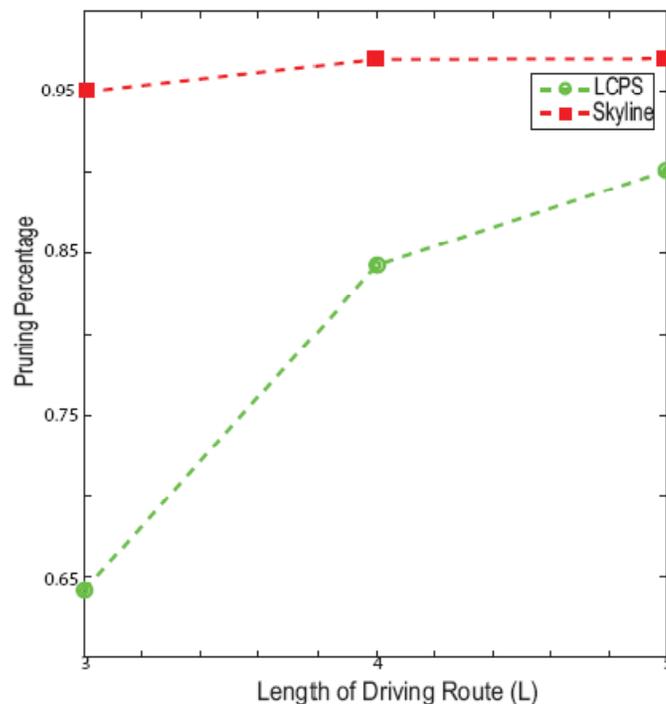
### Some Acronyms.

|           |  |
|-----------|--|
| BFS:      | Brute-Force Search .   |
| LCPS:     | Search with $\mathcal{LCP}$  |
| SR(BNL)S: | Search via Skyline Computing algorithm <i>SkyRoute</i> + <i>BNL</i> .        |
| SR(D&C)S: | Searching via Skyline Computing Algorithm <i>SkyRoute</i> + <i>D&amp;C</i> . |

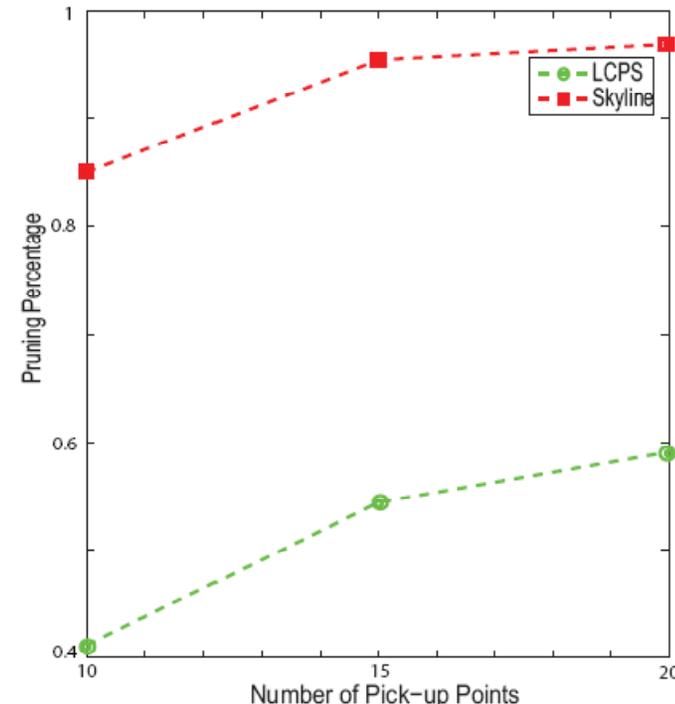
# An Overall Comparison

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## The Pruning Effect



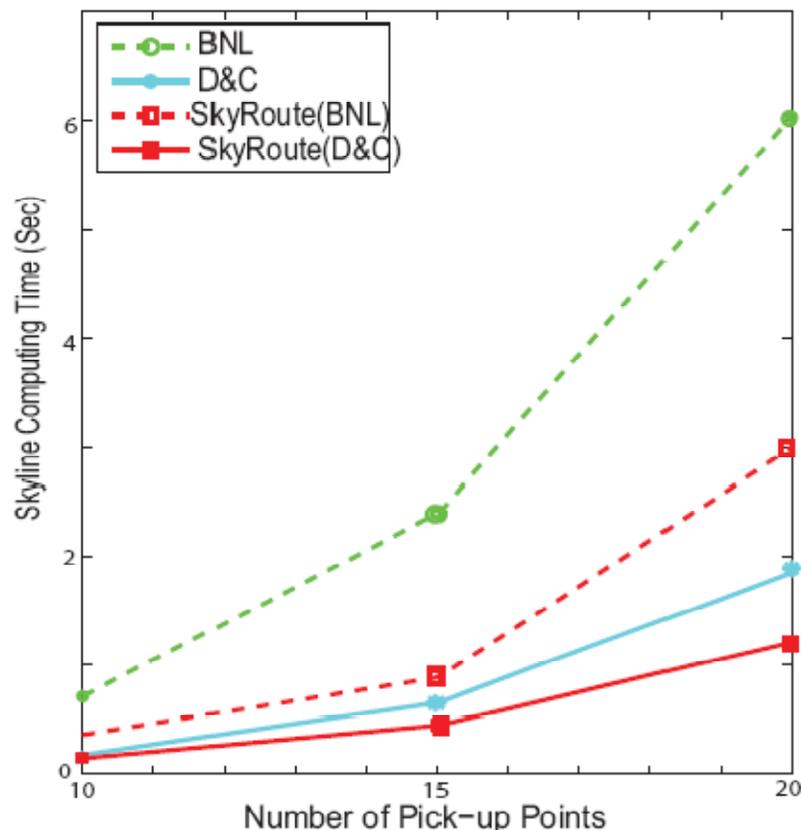
(a) The Pruning Effect on Real Data (6-7PM)



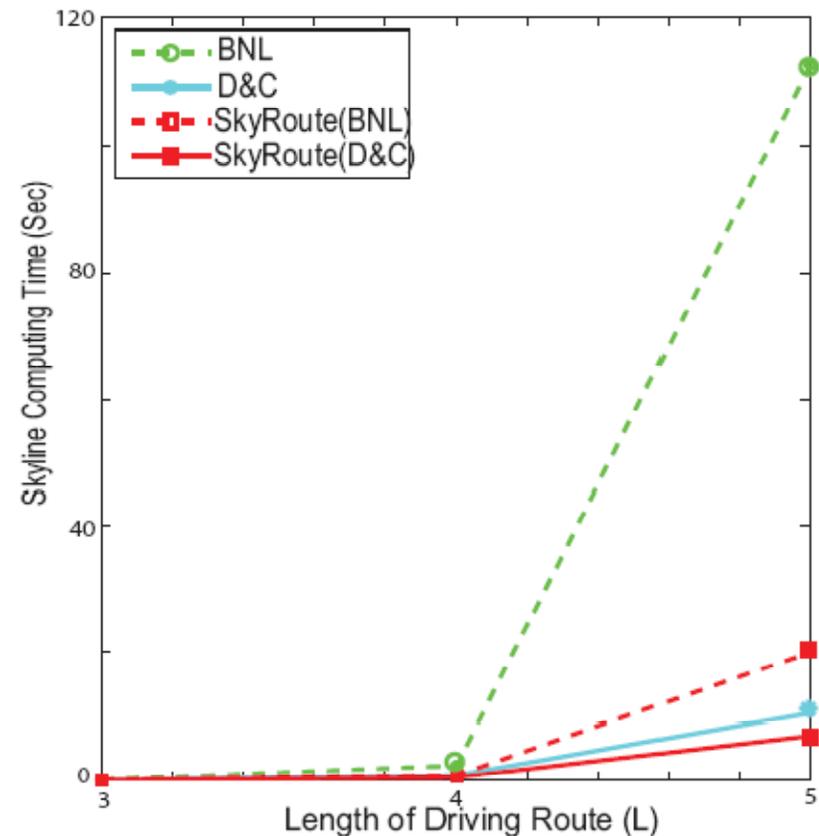
(b) The Pruning Effect on Synthetic Data (L=3)

Pruning percentage: the number of pruned candidates divided by the number of all original candidates

# A Comparison of Skyline Computing



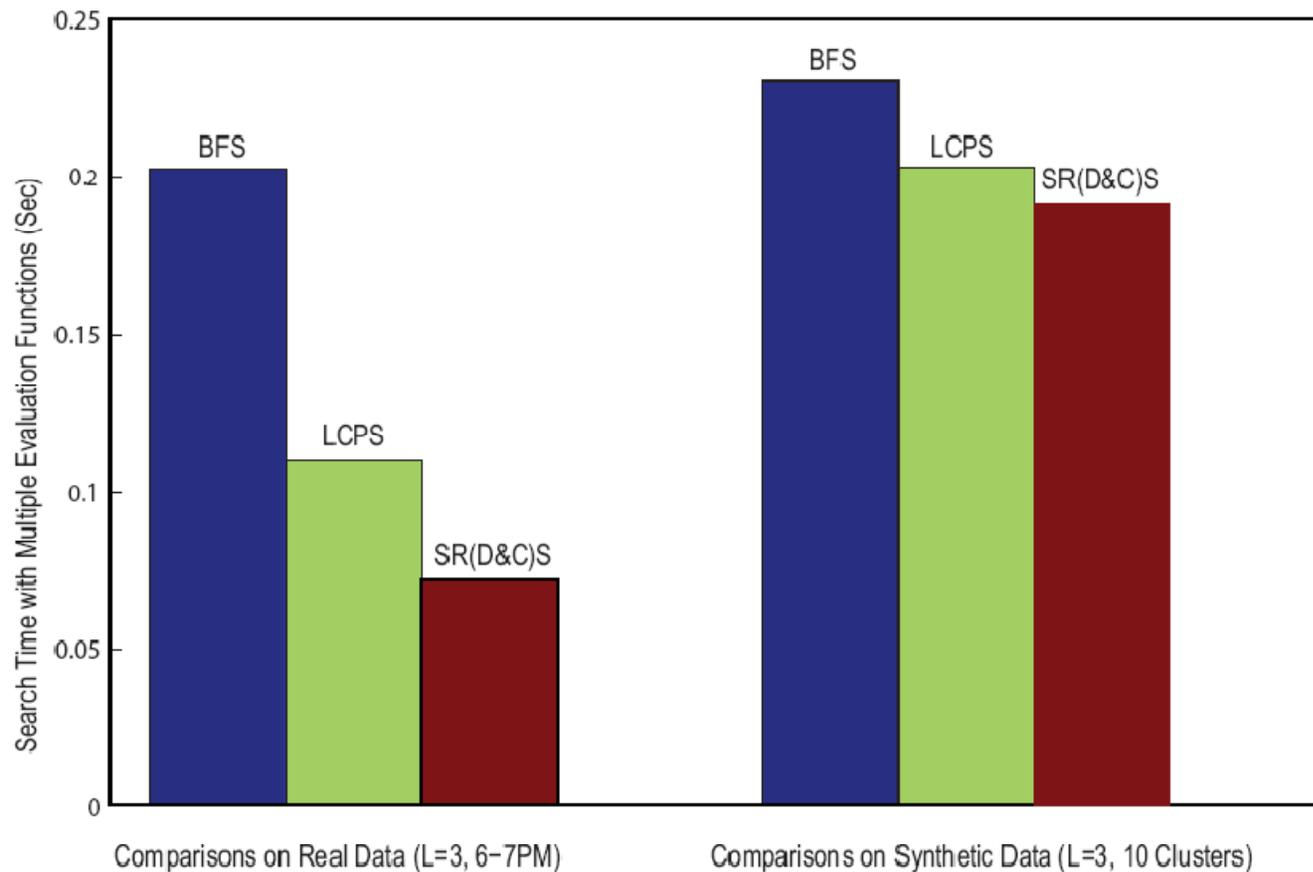
(a) Comparisons on Synthetic Data (L=3)



(b) Comparisons on Real Data (6-7PM)

# Case: Multiple Evaluation Functions

A Comparison of Search Time for Multiple Optimal Driving Routes



Five different evaluation functions

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# Conclusion Remarks

- An energy-efficient mobile recommender system
- Potential Travel Distance (PTD) Function
- Algorithms: *LCP* and SkyRoute

# Thank You !

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Poster Session II & Demo Session  
Date: Tuesday, July 27, 2010  
Time: 5:45pm - 8:00pm  
Location: Independence Center B, floor 1

# The Recommendation Process

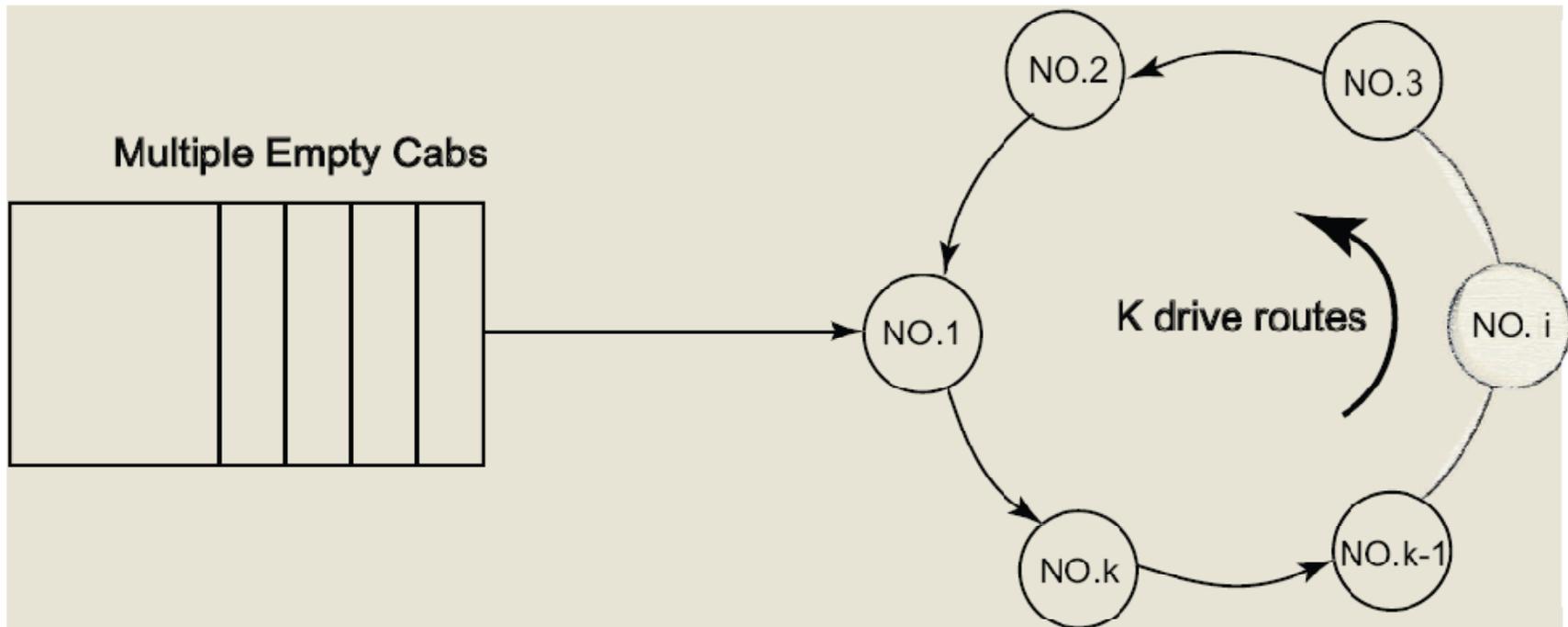


Illustration of the *Circulating Mechanism*

# The *SkyRoute* Algorithm

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**ALGORITHM** *SkyRoute*( $\mathcal{C}, \mathcal{P}, Dist, \mathcal{L}, PoCab$ )

Input:

- $\mathcal{C}$ : set of cluster nodes with central positions
- $\mathcal{P}$ : probability set for all cluster nodes
- $Dist$ : pairwise drive distance matrix of cluster nodes
- $\mathcal{L}$ : the length of suggested drive route
- $PoCab$ : the position of one empty cab

Output:

$\vec{R}_{Skyline}$ : list of skyline drive routes.

**Online Processing**

1. Enumerate all candidate routes by connecting  $PoCab$  with each sub-route of  $\mathcal{R}_{sub}^{\mathcal{L}}$  obtained in step 10 during Offline Processing
2. for  $i = 2 : \mathcal{L} - 1$
3.     Decide dominated sub-routes with  $i$ th intermediate cluster and prune the corresponding candidates by using proposition 2
4.     Update the candidate set by filtering the pruned candidates in step 3
5. end for
6. Select the remained candidate routes with length of  $\mathcal{L}$  from the loop above
7. Final typical skyline query to get  $\vec{R}_{Skyline}$  from those candidate routes in step 6

**Offline Processing**( $\mathcal{LCP}$ )

8. Enumerate all sub-routes with length of  $\mathcal{L}$  from  $\mathcal{C}$
9. Prune and maintain dominated Constrained Sub-routes with length of  $\mathcal{L}$  using proposition 3
10. Maintain the remained non-dominated sub-routes with length of  $\mathcal{L}$ , denoted as  $\mathcal{R}_{sub}^{\mathcal{L}}$

The pseudo-code of SkyRoute Algorithm

- ◆ First use LCP to prune some candidates
- ◆ Gradually prune candidates containing dominated sub-routes

# An Overall Comparison

## A Comparison of Search Time (Second) between BFS and *LCPS*

| 10 Synthetic Pick-up Clusters |                   |                   |                   |
|-------------------------------|-------------------|-------------------|-------------------|
|                               | $\mathcal{L} = 3$ | $\mathcal{L} = 4$ | $\mathcal{L} = 5$ |
| BFS                           | 0.051643          | 0.300211          | 2.000949          |
| <i>LCPS</i>                   | <b>0.043750</b>   | <b>0.165401</b>   | <b>0.803290</b>   |
| 15 Synthetic Pick-up Clusters |                   |                   |                   |
| BFS                           | 0.142254          | 1.925054          | 23.517042         |
| <i>LCPS</i>                   | <b>0.095364</b>   | <b>0.611193</b>   | <b>4.322053</b>   |
| Real Data (2-3PM)             |                   |                   |                   |
| BFS                           | 0.045933          | 0.297187          | 1.991507          |
| <i>LCPS</i>                   | <b>0.036736</b>   | <b>0.141536</b>   | <b>0.622932</b>   |

# An Overall Comparison

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A Comparison of Search Time ( $\mathcal{L} = 3$ ) on the Synthetic Data set

